



H2020 Marie Skłodowska-Curie  
innovative training network

**Workshop:  
Missing Data & Longitudinal Models in Mplus**

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### Who are you?

- What experience have you with Structural Equation Modeling (SEM) so far?
  - 12% no experience; 36% beginners; 40% occasional users; 12% experienced users
- Have you used Mplus before?
  - 13% no; 87% yes
- Have you used Mplus before to analyze longitudinal data?
  - 48% no; 52% yes
- What is your main learning objective today?
  - 21% curious about SEM and Mplus; 74% learning SEM and Mplus for longitudinal data; 10% my advisor requires me; 36% complex data; 10% latent variable stuff

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### With special thanks to...

Luc Goossens



Tod Little



Patrick Curran



Karl Jöreskog

Bengt & Linda Muthén  
(no pics available)

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*Change is inevitable. Change is constant.*  
(Benjamin Disraeli)

*Change is the nursery of music, joy, life, and eternity.*  
(John Donne)

*When you're finished changing, you're finished.*  
(Benjamin Franklin)

*We are restless because of incessant change, but we would be frightened if change were stopped.*  
(Lyman Bryson)

*Change is a measure of time.*  
(Edwin Way Teale)



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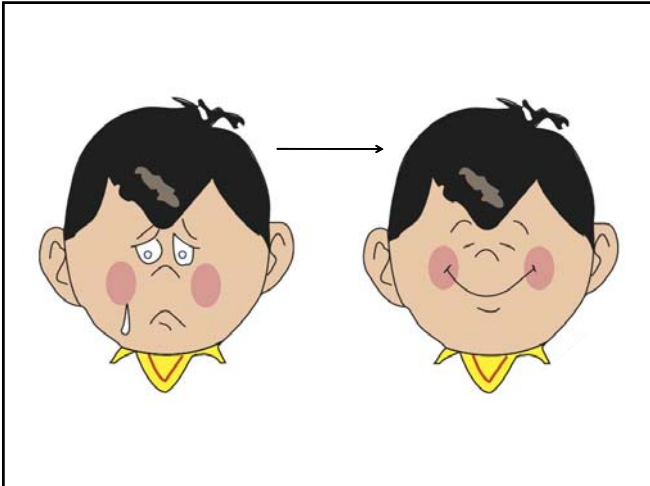
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**DEVELOPMENT**

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- General measurement and design issues
  - Time & Intervals
  - Differential growth
  - Missing values
- General measurement and design issues
  - Time and intervals
  - Differential growth
  - Missing values
- Classic methods and disadvantages
  - Difference score
  - Repeated ANOVA
  - Autoregression
  - Cross-lagged models
- Classic methods and disadvantages
  - Absolute change: the difference score
  - Absolute change+: repeated measures ANOVA
  - Relative change: autoregression
  - Relative change+: cross-lagged models
- New(er) methods
  - LCM
  - LGCM
  - LCGA
  - LGMM
  - LTA
- New(er) methods
  - With 2+ waves: LCM
  - With 3+ waves: LGCM + extension
  - With 3+ waves: LCGA
  - With 4+ waves: LGMM
  - With 3/4+ waves: LTA (mover-stayer)
- Exercise !

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  - Exercise !
- The example DATA**
- N = 405 adolescents + mothers
  - From three cohorts
    - 1: M<sub>age</sub> = 13 at Time 1
    - 2: M<sub>age</sub> = 15 at Time 2
    - 3: M<sub>age</sub> = 17 at Time 3
  - Measures:
    - Time 1:
      - Gender: 203 boys (1) and 202 girls (0) (A-report)
      - Support from mother (A-report) 1-6 3.00 (0.80)
      - Structure by mother (A-report) 1-6 3.29 (0.96)
      - Shaming by mother (A-report) 1-6 2.49 (0.82)
    - Time 1-2-3-4 (yearly measurement):
      - Antisocial behavior (M-report) 0-10 1.66 - 1.83 - 2.03 - 2.06
      - School GPA on PE-class (A-report) 0-10 2.52 - 4.08 - 5.00 - 5.77
    - Missing data (coded 9999):
      - dropout and nonresponse from T3 onwards!
      - from 7% (ANTI-3) to 34% (GPA-4)
      - 11% overall
- [SEM DATA.SAV](#)  
[SEM DATA.DAT](#)  
[SEM DATA.XLS](#)

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  - Exercise !
- When measuring CHANGE, how can we define TIME?
    - Age in years, months, days.
    - **Experiential time:** Amount of time something is experienced
      - Years of schooling (grade), length of relationship, amount of practice
      - Calibrate on beginning of event, measure time experienced
    - **Episodic time:** Time of onset of a life event
      - Age, toilet trained, driver license, puberty, birth of child, retirement
      - Early onset, on-time, late onset: used to classify or calibrate
      - Time since onset or time from normative or expected occurrence.
  - What measurement Intervals should we take?
    - How fast is the developmental process?
    - Intervals must be equal to or less than expected processes of change (e.g., schooling studies at half-year intervals)
    - If too short: too sensitive to measurement error
    - If too long: insensitive to change and variability in change
- A great example article:  
 Reuter & Conger (1998). doi: 10.1037/0012-1649.34.6.1470

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- Exercise !

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- Exercise !

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## Missing data

- What is the problem?
- Types of missing data?
- Preventing
- Curing
  - Bad methods
  - Questionable methods
  - Good methods

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**DROPOUT/MISSING VALUES**

- General measurement and design issues
  - Time & Intervals
  - Differential growth
  - Missing values
- Classic methods and disadvantages
  - Difference score
  - Repeated ANOVA
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- Exercise !

- Aim of statistic analyses =
  - based on sample data, draw conclusions about a population
  - estimate the population parameters as good as possible, based on the sample data
- What if we have incomplete data?
  - Can we still estimate correctly the population parameters?
  - Can we still draw correct conclusions about the population?

→ Missing values!

- occur in about very empirical study
- particularly in longitudinal research (dropout)!

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**TYPES of MISSING VALUES**

- General measurement and design issues
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  - Differential growth
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- Exercise !

- Missing Completely at Random (MCAR)
  - No relationship of missingness with non-observed (missing) data, and no relationship with observed data (= completely a-selective dropout)
- Missing at Random (MAR) !
  - No relationship of missingness with non-observed (missing) data, but possibly (and preferably) a relationship with observed data
- Missing Not at Random (MNAR)
  - A relationship of missingness with non-observed (missing) data (and possibly also with observed data)

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gpa4	gpa4_MCAR	test_MCAR	gpa4_MAR	test_MAR	gpa4_MNAR	test_MNAR
4,50	4,50	0	-.999999	1	-.999999	0
4,60	-.999999	0	4,60	0	-.999999	1
6,20	6,20	0	-.999999	1	6,20	0
4,00	-.999999	1	4,00	0	-.999999	1
7,50	-.999999	0	7,50	0	7,50	0
6,90	6,90	0	6,90	0	6,90	0
6,10	6,10	0	6,10	0	-.999999	1
4,20	-.999999	1	-.999999	1	-.999999	1
6,30	6,30	0	6,30	0	6,30	0
7,20	7,20	0	7,20	0	7,20	0
5,80	5,80	0	5,80	0	-.999999	1
5,80	-.999999	1	5,80	0	5,80	0

test_MCAR	Pearson Correlation	gpa4	gpa1	support
		-.038	,017	-.077
	Sig. (2-tailed)	,576	,798	,252
	N	221	221	221

test_MAR	Pearson Correlation	support	gpa1	gpa4
		,266	-.079	-.009
	Sig. (2-tailed)	,000	,241	,689
	N	221	221	221

test_MNAR	Pearson Correlation	support	gpa1	gpa4
		-.067	-.188	-.399
	Sig. (2-tailed)	,320	,005	,000
	N	221	221	221

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**DROPOUT**

X (wave1)	Y (wave 2)			
	Complete	MCAR	MAR	MNAR
130	101	101	101	101
145	155			
136	140	140	140	
146	134	134		134
111	129		111	129
134	124		124	124
153	112			112
137	122	122	122	122
118	118	118	118	118

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- Exercise !

• How to test for?

- Not really possible. But...
- MVA (SPSS) →

• References:

- Little & Rubin (2002). *Statistical analysis with missing data*. Wiley
- Schafer & Graham (2002): doi: 10.1037/1082-989X.7.2.147

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Table with **Separate Variance t Test** in output, with in rows all variables with (+5%) missings, and in columns all variables in dataset. Cell contain a t-value (+ p) indicating whether or not missingness in the row variable is correlated significantly with the values of the column variable, and therefore is selective. Check patterns of significant t-values. If not clear pattern, MAR is very likely!

When selecting EM in the 'Estimation' -menu, Little's MCAR test is provided (= summary of t-tests above). If not significant: MCAR! If  $X^2/df$  (normed  $X^2$ ) < 2: MAR.

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**PREVENTING DROPOUT & MNAR!**

- General measurement and design issues
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- Exercise !

- **Dillman (1978)**
  - ✓ Intensive follow-up and tracking of subjects
  - ✓ Repeated invitations to participation, reminders
  - ✓ Repeated sending of the measurements
  - ✓ Do everything to prevent large dropout!
- **Planned missingness**
  - ✓ Do not measure all variables in all participants at all times.
- **Cohort-sequential design!!**
  - ✓ Let new persons come in at each wave of the study,
  - ✓ This way you create different patterns of missingness, not only dropout!

**= Different ways to increase the chances of MAR or MCAR!**

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**CURING!**

- Purpose is NOT to fill in empty cells in the data!
- Purpose IS to estimate the population parameters as good as possible, using a sample with missing data!

**Which methods can help us in this challenging task?**

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- Exercise !

**BAD ways to deal with missing data**

- **List-wise Deletion**
  - Variances biased, means biased
  - *Acceptable only if power is not an issue and the incomplete data is MCAR*
- **Pair-wise Deletion**
  - *N* varies for each correlation
  - Variances biased, means biased
  - Sometimes estimation problems!
  - *Acceptable only if power is not an issue and the incomplete data is MCAR*
- **Sample-wise Mean Substitution**
  - For long time very popular method!
  - Variances reduced, correlations biased
  - *Never acceptable!*
- **Subject-wise Mean Substitution**
  - Depends on homogeneity of the items used
  - *Acceptable only if set of items is homogeneous and only few missings!*

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**QUESTIONABLE ways to deal with missing data (single imputation methods)**

- **Regression Imputation**
  - All subjects with same values on IVs get the same estimated value on the DV.
  - Variances reduced
  - *Assumes MCAR*
- **Stochastic Regression Imputation**
  - Same as above but a random error component is added to reduce the loss in variance
  - *Still assumes MCAR*

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- General measurement and design issues
  - Time & Intervals
  - Differential growth
  - Missing values

**GOOD ways to deal with missing data**

- But only if enough variables related to missingness are included in analysis (MAR), or missingness is MCAR

- Classic methods and disadvantages
  - Difference score
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  - Autoregression
  - Cross-lagged models

**EM Imputation**

- Imputes the missing data values in an iterative way, starting with the E step
- The E(stimation)-step is a stochastic regression-based imputation for each variable.
- The M(aximization)-step is to calculate a complete covariance matrix based on the estimated values.
- The E-step is repeated for each variable but the regression is now on the covariance matrix estimated in the previous M-step.
- The EM-steps are repeated until the imputed estimates don't differ from one iteration to the other

- New(er) methods
  - LCM
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• Exercise !

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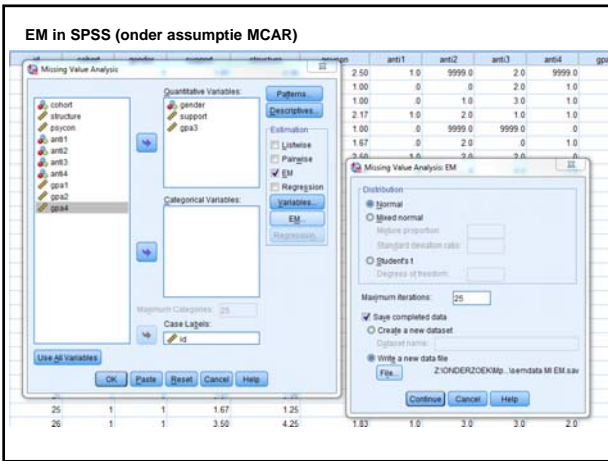
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**EM in SPSS (under assumptie MCAR)**




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**EM in SPSS (under assumptie MCAR)**

Univariate Statistics

	N	Mean	Std. Deviation	Missing		No. of Extremes <sup>a</sup>	
				Count	Percent	Low	High
gender	405	.50	.501	0	.0	0	0
support	405	3.0074	.80219	0	.0	22	7
gpa3	275	5.005	1.1610	130	32.1	0	2

a. Number of cases outside the range (.01 - 1.5\*IQR, 0.3 - 1.5\*IQR).

**EM Means<sup>a</sup>**

	gender	support	gpa3
gender	.50	3.0074	4.997

a. Little's MCAR test, Chi-Square = 2.512, DF = 2, Sig. = .285

**EM Covariances<sup>a</sup>**

	gender	support	gpa3
gender	.251		
support	-.026	.64351	
gpa3	-.028	.15530	1.3492

a. Little's MCAR test: Chi-Square = 2.512, DF = 2, Sig. = .285

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**EM in SPSS (onder assumptie MAR)**

Missing Value Analysis dialog box showing the selection of variables (cohort, gender, support, structure, psycon, an1, an2, an3, an4, gpa1) and the EM method. The Distribution tab shows 'Mixed normal' selected, with 'Maximum iterations' set to 100 and 'Save completed data' checked.

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**EM in SPSS (onder assumptie MAR)**

	N	Mean	Std. Deviation	Missing		No. of Extremes <sup>a</sup>	
				Count	Percent	Low	High
cohort	405	2.00	.818	0	0	0	0
gender	405	.50	.501	0	0	0	0
support	405	3.0074	.80219	0	0	22	7
structure	405	3.2628	.86177	0	0	34	1
psycon	405	2.4859	.82896	0	0	0	27
an1	405	1.662	1.6581	0	0	0	1
an2	297	1.838	1.6979	108	26.7	0	4
an3	374	2.027	2.0370	31	7.7	0	6
an4	294	2.061	2.1520	111	27.4	0	6
gpa1	405	2.523	.9249	0	0	0	8
gpa2	375	4.076	1.0836	30	7.4	0	3
gpa3	375	5.095	1.1610	130	32.1	0	2
gpa4	270	5.774	1.2480	135	33.3	0	0

a. Number of cases outside the range (Q1 - 1.5\*IQR, Q3 + 1.5\*IQR)

EM Means <sup>a</sup>												
cohort	gender	support	structure	psycon	an1	an2	an3	an4	gpa1	gpa2	gpa3	gpa4
2.00	.50	3.0074	3.2628	2.4859	1.662	1.890	1.989	2.188	2.523	4.068	5.023	5.601

a. Little's MCAR test: Chi-Square = 330.094, DF = 266, Sig. = .005

Ook beschikbaar in Lisrel (Preliis), SAS (PROC MI, met OUTEM= optie), e.a.

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- Exercise !

**GOOD ways to deal with missing data**

- But only if enough variables related to missingness are included in analysis (MAR), or missingness is MCAR
- Multiple Imputation
  - Estimate  $N$  (e.g., 5) datasets using the EM algorithm
  - Each dataset is based on a kind of resampling of the original sample (equivalent to a random selection of a different sample from the population)
  - Possible way 1:
    - Run the analyses  $N$  times
    - Summarize the results of these  $N$  analyses using the formulas of Rubin (1987)
  - Possible way 2:
    - Collapse the  $N$  samples to one dataset and do the analyses.

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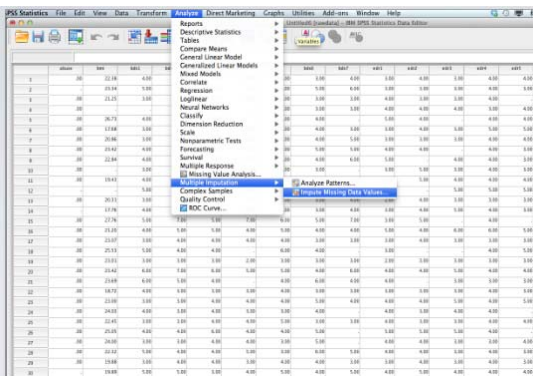
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## MI in SPSS




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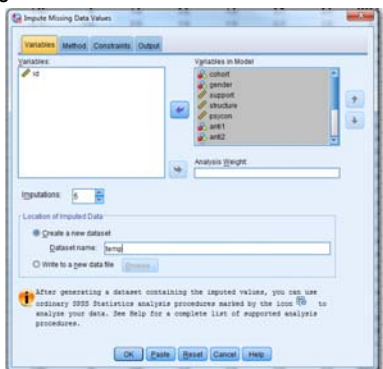
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## MI in SPSS



Further info at [www.appliedmissingdata.com/spss-multiple-imputation.pdf](http://www.appliedmissingdata.com/spss-multiple-imputation.pdf)

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## MI in Mplus

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Mplus -[ex15img]
File Edit View Mplus Plot Diagram Window Help

TITLE: this is an example of multiple imputation for a set of
variables with missing values
DATA: FILE = seshdata.dat;
VARIABLES: ! the following are all the variables in the data set:
          NAMES = id cohort gender support structure paycom
                ant1 ant2 ant3 ant4 opa1 opa2 opa3 opa4;
! the following variables will be used to create the
! imputed data sets.
USEVARIABLES = ant12 ant13 ant14 opa2 opa3 opa4;
! the following variables are saved with the imputed
! data sets, but not used to create the imputed data
! sets:
AUXILIARY = id cohort gender support structure paycom
            ant1 opa1;
MISSING = ALL (9999);

DATA IMPUTATION:
! the following are the variables for which missing
! data will be imputed:
IMPUTE = ant12 ant13 ant14;
MDATESETS = 10;
! the following immediately runs a model on this MI data
! and pools the estimates
ANALYSIS: ESTIMATOR = ML;
MODEL: ant14 ON ant12 opa2;
OUTPUT: TECH1;
    
```

Further info at <https://www.statmodel.com/download/Imputations7.pdf>

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**GOOD ways to deal with missing data**

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- Classic methods and disadvantages
  - Difference score
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  - LTA
- Exercise !

- **But only if enough variables related to missingness are included in analysis (MAR), or missingness is MCAR, but even in cases of MNAR!**
- **Full Information Maximum Likelihood (FIML)**
  - Sufficient statistics (means, covariances) are estimated with the Expectation Maximization (EM) algorithm
  - Those estimates then serve as the start values for the Maximum Likelihood model estimation
  - Does not impute the missing values.
  - Can only be used when testing a SEM-model.
  - Available in Lisrel, AMOS, *Mplus*, EQS, etc.

EXAMPLES comes with LGC and other models.

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**Missing values: Conclusions**

- General measurement and design issues
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- Exercise !

- Missing values are part of every empirical study.
- Neglecting the missing data (listwise deletion) is a wrong approach.
- Different good methods are available to handle data that are MAR or MCAR, and give us correct population parameters!
- Even methods are available in case data are MNAR!

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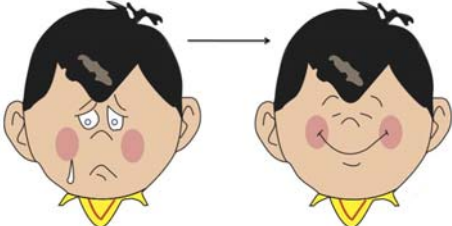
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**How to analyze change?**

- Classic methods & disadvantages
- New(er) & better methods, using SEM




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**CHANGE<sub>t4</sub> = ANTI<sub>t4</sub> - ANTI<sub>t1</sub>**

- General measurement and design issues
  - Measurement
  - Time & Intervals
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- Exercise !

• Though many problems with it, still popular (e.g., intervention, pretest-posttest, or clinical studies)

• Most cited problem: Unreliability of the difference score

- when the measures comprising the difference are only modestly reliable and positively correlated →
- which is typically the case in longitudinal research!

• And therefore also: lack of validity

+ Change is measured without taking level into account!

difference score.inp

```
DEFINE: changel4 = anti4-antil;
MODEL: changel4 ON support;
```

	Estimate	S.E.	Est./S.E.	Two-Tailed P-Value
CHANGE14 ON SUPPORT	-0.038	0.183	-0.207	0.836

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r <sub>2</sub>	0.60	0.70	0.80	0.90	1.00
	r <sub>1</sub> = 0.60				
0.60	0.00	0.13	0.25	0.38	0.50
0.70	-0.33	-0.17	0.00	0.17	0.33
0.80	-1.00	-0.73	-0.50	-0.25	0.00
0.90	-	-	-	-	-1.00
0.95	-	-	-	-	-
	r <sub>1</sub> = 0.70				
0.60	0.13	0.25	0.38	0.50	0.63
0.70	-0.17	0.00	0.17	0.33	0.50
0.80	-0.75	-0.50	-0.25	0.00	0.25
0.90	-	-	-	-1.00	-0.50
0.95	-	-	-	-	-
	r <sub>1</sub> = 0.80				
0.60	0.25	0.38	0.50	0.63	0.75
0.70	0.00	0.17	0.33	0.50	0.67
0.80	-0.50	-0.25	-0.125	0.25	0.50
0.90	-	-	-	-1.00	-0.50
0.95	-	-	-	-	-
	r <sub>1</sub> = 0.90				
0.60	0.38	0.50	0.63	0.75	0.88
0.70	0.17	0.33	0.50	0.67	0.83
0.80	-0.25	0.00	0.25	0.50	0.75
0.90	-	-	-1.00	0.00	0.50
0.95	-	-	-	-1.00	0.00
	r <sub>1</sub> = 1.00				
0.60	0.50	0.63	0.75	0.88	1.00
0.70	0.33	0.50	0.67	0.83	1.00
0.80	0.00	0.25	0.50	0.75	1.00
0.90	-	-1.00	0.00	0.50	1.00
0.95	-	-	-1.00	0.00	1.00

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**CHANGE<sub>t4</sub> = ANTI<sub>t4</sub> - ANTI<sub>t1</sub>**

- General measurement and design issues
  - Measurement
  - Time & Intervals
  - Differential growth
  - Missing values
- Classic methods and disadvantages
  - Difference score
  - Repeated ANOVA
  - Autoregression
  - Cross-lagged models
- New(er) methods
  - LCM
  - LGCM
  - LCGA
  - LGMM
  - LTA
- Exercise !

• Though many problems with it, still popular (e.g., intervention, pretest-posttest, or clinical studies)

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• And therefore also: lack of validity

+ Change is measured without taking level into account!

difference score.inp

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**CHANGE = effect of TIME in a repeated ANOVA**

- General measurement and design issues
  - Measurement
  - Time & Intervals
  - Differential growth
  - Missing values
- Classic methods and disadvantages
  - Difference score
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- Exercise !

- SPSS output: [R ANOVA.spv](#)
- So, a good method
  - To describe and test an overall mean change function, and test for the form of it (linear, quadratic, cubic, etc.)
  - To test for the effect of covariates on the change function (e.g., support): Time x Support interactions!
  - To test for the effect of between-subject factors on the change function (e.g., gender): Time x Gender interactions!
- But
  - Only tests mean change over time in the whole sample and not deviations from that mean change
  - And... group statistics (e.g., mean) represent everyone, and no one!
  - Equal intervals between measurements are necessary!
  - Change is an outcome of the repeated measures (time) and cannot be used as a predictor of outcomes.

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- Exercise !

- With observed variables: [autoregression.inp](#)
- With latent variables! [autoregression.latent.inp](#)

- But...
  - implicit assumption of decreasing correlations across time!
  - indifferent to the functional form of change!
  - only RELATIVE change in terms of rank order!
  - Interpretation?
    - Does ANTI1 predict (.86) an increase in ANTI4?
    - Increase only relative to others in the sample!
    - Even if everyone decreases!
  - No trajectories of individual change over time!

Extensions: mediation: [autoregressionb.inp](#)  
 moderation: [autoregression-multigroup.inp](#)

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- Exercise !

- A multivariate extension of the autoregressive model of change: [crosslagged.inp](#)

Antisocial behavior is 'causing' change in GPA!

- Interesting for examining direction of effects, by comparing cross-lagged coefficients (easily done in SEM)
- But
  - Same problem with interpretation of change as in AR model!
  - Also shares all other problems of the AR model!
  - + Statistical drawbacks:
    - If X is (much) more stable than Y, then Y will have a stronger effect on X than vice versa!
    - And, the less reliable X is, the less Y can explain it.

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- Exercise !

So,

What do we want exactly when we try to assess change?

RELIABLE estimates of change!  
Estimates of ABSOLUTE change!  
INDIVIDUAL estimates of change!

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- Exercise !

**With 2 WAVES of data**

**Latent Change Models (LCM)**  
(McArdle & Nesselrode, 1994; Hertzog & Nesselrode, 2003)

- Change in **latent** variables, using (CFA)
- First step = Longitudinal invariant factor model (multiple indicators), resulting in reliable scores for Anti-1 and 4. →
- Second step = Restructuring Anti-1 and Anti-4 in latent Level and Change factors, using a very simple equation:
 
$$\text{Anti-1} = 1 \times \text{Anti-Level}$$

$$\text{Anti-4} = 1 \times \text{Anti-Level} + 1 \times \text{Anti-Change}$$
- As a consequence:
 
$$\text{Anti-Change} = \text{Anti-4} - \text{Anti-1}$$

$$\text{Anti-Level} = \text{Anti-1}$$

↓  
a reliable difference score !

• [lcm\\_ANTLinp](#)

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## Observed variables?

The problem of measurement error  
**DATA = MODEL + ERROR**

error  
true

↔

error  
true

- True variance: correlated
- Error variance: not correlated
- Total covariance: underestimated!

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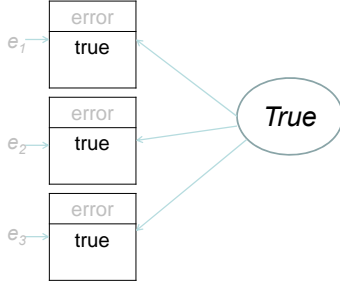
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## Latent variables!

Solution for measurement error!



SEM = analysis with latent variables!

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### General measurement and design issues

- Measurement
- Time & Intervals
- Differential growth
- Missing values

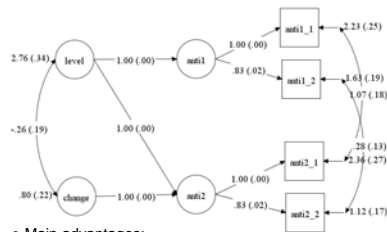
### Classic methods and disadvantages

- Difference score
- Repeated ANOVA
- Autoregression
- Cross-lagged models

### New(er) methods

- LCM
- LGCM
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- LTA

### Exercise !



### Main advantages:

- Only two waves of data needed!
- Can be extended to multiple successive change factors!
- Reliable estimates of change!
- Change is assessed as a latent factor!
  - With a mean: Mean change in the total sample!
  - With a variance: Individual differences in change!
  - That can be predicted and used as a predictor!
  - Latent factor scores can be estimated!

### But

- Only linear change function!

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### General measurement and design issues

- Measurement
- Time & Intervals
- Differential growth
- Missing values

### Classic methods and disadvantages

- Difference score
- Repeated ANOVA
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### Exercise !

### With 3+ WAVES of data

#### Latent Growth Curve Models (LGCM)

(Duncan et al., 1994; McArdle & Nesselroade, 2002; Willet & Sayer, 1994)

### Questions:

- Does an individual characteristic (e.g., antisocial behavior) change over time?
- Which trajectory is followed?
- Interindividual differences?

### Step 1: Within-Person

- Equation for every subject in the sample:  

$$anti = \text{intercept} + (\text{slope} \times \text{Time}) + \text{error} \quad (\text{regression})$$
- Growth can be non-linear too!  

$$anti = \text{intercept} + (\text{slope} \times \text{Time}) + (\text{curve} \times \text{Time}^2) + \text{error}$$
- Assumption: Individuals share the shape of the change function (e.g., linear), but can differ in the amount or rate of change (individual growth parameters: intercept, slope, etc.)

### Step 2: Between-Person

- Means (fixed) & variances (random) of intercepts, slopes
- Predictors of change (conditional growth models).

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**With 3+ WAVES of data**

**Latent Growth Curve Models (LGCM)**  
 (Duncan et al., 1994; McArdle & Nesselroade, 2002; Willet & Sayer, 1994)

**anti**

**time (age)**

- General measurement and design issues
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- Exercise !

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**With 3+ WAVES of data**

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**With 3+ WAVES of data**

**Latent Growth Curve Models (LGCM)**  
 (Duncan et al., 1994; McArdle & Nesselroade, 2002; Willet & Sayer, 1994)

**anti = 2 + (1.5 x time) + error**

**anti**

**time (age)**

- General measurement and design issues
  - Measurement
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**With 3+ WAVES of data**

**Latent Growth Curve Models (LGCM)**  
(Duncan et al., 1994; McArdle & Nesselroade, 2002; Willet & Sayer, 1994)

$\text{anti} = 1 + (1.5 \times \text{time}) + (.5 \times \text{time}^2) + \text{error}$

anti

time (age)

- General measurement and design issues
  - Measurement
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Exercice !

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Exercice !

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**Two Approaches to GCM**

Multilevel	SEM: LGCM
- regression approach	- factor approach
- fixed & random effects	- means & variances
- flexible with missing values & individual-varying intervals	- not that flexible with individual-varying intervals
- less flexible in prediction	- very flexible in prediction
$\text{length} = b_{0i} + b_{0i} \times \text{gender} + \text{error}_i + (b_{1i} + b_{1i} \times \text{gender} + \text{error}_i) \times \text{time} + \text{error}$	
- little attention for model fit	- overload of fit indices

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Exercice !

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**With 3+ WAVES of data**

**Latent Growth Curve Models (LGCM)**  
(Duncan et al., 1994; McArdle & Nesselroade, 2002; Willett & Sayer, 1994)

**PARAMETERS in the model**

- Mean intercept / fixed effect intercept  
= Mean initial level of all individuals
- Variance intercept / random effect intercept  
= Interindividual differences in initial level
- Mean slope / fixed effect slope  
= Mean rate of growth across individuals
- Variance slope / random effect slope  
= Interindividual differences in rate of change

[lgcm\\_anti.inp](#) (with missing data, and FIML)

- General measurement and design issues
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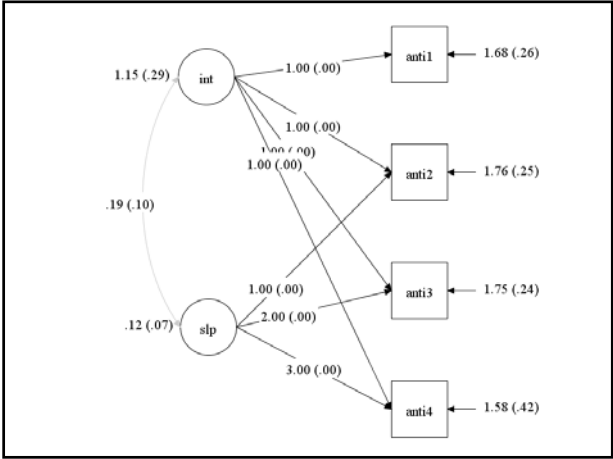
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**With 3+ WAVES of data**

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= Mean rate of growth across individuals
- Variance slope / random effect slope  
= Interindividual differences in rate of change

[lgcm\\_anti.inp](#) (with missing data, and FIML)

[lgcm\\_anti + predictors.inp](#) (gender and support as predictors)

[lgcm\\_anti + predictors + interaction.inp](#) (support X level anti)

[lgcm\\_anti - piecewise.inp](#) (piecewise model with 2 slopes)

- General measurement and design issues
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**With 3+ WAVES of data**

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- Exercise !

- Can be extended to a multivariate LGCM!  
[lgcm\\_anti + qqa.inp](#)
  - Correlated intercepts = cross-sectional association
  - Correlated intercept & slope = level of IV is predicting rates of change in DV!
  - Correlated slopes = common underlying growth in two constructs = change associated with change (causality?)
- But
  - Assumption: same shape of the growth function for all subjects; interindividual differences in change are modeled as deviations from that overall mean.

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**With 3+ WAVES of data**

**Latent Growth Curve Models (LGCM)**  
(Duncan et al., 1994; McArdle & Nesselroade, 2002; Willet & Sayer, 1994)

**Extension: Cohort sequential design!**

= mixing cross-sectional & longitudinal design

- remember: CS-design → MAR
- Many longitudinal studies have multiple cohorts.
- Example: PhD of 4 years, but wanting to measure antisocial behavior from age 13 to 20 (8 years)!

Cohort	Time			
	T1	T2	T3	T4
1 (1985)	13	14	15	16
2 (1983)	15	16	17	18
3 (1981)	17	18	19	20

- General measurement and design issues
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- Exercise !

→ Linking adjacent segments of change from different cohorts to estimate a common growth curve

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**With 3+ WAVES of data**

**Latent Growth Curve Models (LGCM)**  
(Duncan et al., 1994; McArdle & Nesselroade, 2002; Willet & Sayer, 1994)

**Extension: Cohort sequential design!**

Method 1: Multigroup modeling

Cohort	Time			
	T1	T2	T3	T4
1 (1985)	13	14	15	16
2 (1983)	15	16	17	18
3 (1981)	17	18	19	20

- General measurement and design issues
  - Measurement
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- Exercise !

- Growth curve for each cohort, but:
  - Fix mean and variance of intercept and slope equal across cohorts
  - Fix int-slp correlation equal across cohorts
  - Adjust slope factor loadings of anti in line with cohort or birthyear
    - Cohort 1 (1985): 0 1 2 3
    - Cohort 2 (1983): 2 3 4 5
    - Cohort 3 (1981): 4 5 7 8

[cohort-sequential growth model anti.inp](#) (linear)  
[cohort-sequential growth model anti.inp](#) (curvilinear)

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**With 3+ WAVES of data**

**Latent Growth Curve Models (LGCM)**  
(Duncan et al., 1994; McArdle & Nesselroade, 2002; Willet & Sayer, 1994)

**Extension: Cohort sequential design!**

Method 2: Data rearrangement (DATA COHORT)

Cohort	Age							
	13	14	15	16	17	18	19	20
1 (1985)	X	X	X	X	MCAR	MCAR	MCAR	MCAR
2 (1983)	MCAR	MCAR	X	X	X	X	MCAR	MCAR
3 (1981)	MCAR	MCAR	MCAR	MCAR	X	X	X	X

- Estimate 1 intercept and 1 slope, using all available data
  - Works out the time score based on birth and measurement year
  - Idea = rearrange our cohort & time data to age data
  - Then a growth curve for the complete age span!
  - Only works with continuous variables!

[cohort-sequential growth model anti 2a.inp](#) (linear)  
[cohort-sequential growth model anti 2b.inp](#) (curvilinear)  
 !? [cohort-sequential growth model anti 2 piecewise.inp](#)

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**With 3/4+ WAVES of data**

**Latent Growth Mixture Modeling (LGMM)**  
(Muthén, 2001, 2004)

and a special case of it:  
**Latent Class Growth Analysis (LCGA)**  
(Nagin, 1999, 2001)

- Cfr. LGCM: heterogeneity in the sample is captured by variation around a mean growth function, i.e., it is assumed that all individuals are drawn from the same population.
- LGMM
  - relaxes this single population assumption to allow for parameter differences across unobserved subpopulations
  - by using a combination of continuous and categorical latent variables (mixed)
  - by introducing a latent class variable C, a trajectory class variable, representing k unobserved subpopulations in the sample (note that in LGCM k = 1)
  - by estimating a separate growth model for each of the latent classes
  - and estimating latent class conditional probabilities (membership)

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**With 3/4+ WAVES of data**

**Latent Growth Mixture Modeling (LGMM)**  
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**With 3/4+ WAVES of data**  
**Latent Growth Mixture Modeling (LGMM)**  
**Latent Class Growth Analysis (LCGA)**

- General measurement and design issues
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- Exercise !

- **LGMM:** Class differences
  - Typically between mean intercepts between classes
  - Mean slopes in the classes
  - Variance in intercept and slope
  - Shape of the growth function!
  - Influence of covariates!
- **LGMM:** Extensions
  - Including covariates of change
  - Including outcomes that are predicted from growth
- **LCGA** (Nagin)
  - Very similar, only no variances within classes are estimated (therefore a semi-parametric approach)
  - Individuals within classes are treated as homogeneous

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**With 3/4+ WAVES of data**  
**Latent Growth Mixture Modeling (LGMM)**  
**Latent Class Growth Analysis (LCGA)**

- General measurement and design issues
  - Measurement
  - Time & Intervals
  - Differential growth
  - Missing values
- Classic methods and disadvantages
  - Difference score
  - Repeated ANOVA
  - Autoregression
  - Cross-lagged models
- New(er) methods
  - LCM
  - LGCM
  - LCGA
  - LGMM
  - LTA
- Exercise !

- Estimation: Using the EM algorithm
  - Estimation of each individual's probability of membership in each class (conditional probabilities)
  - Measures of fit and classification quality:
    - BIC
      - Small values correspond to a good model with a large likelihood and not too many parameters
      - Look at the big drops in BIC from one solution to another!
      - Sensitive to the number of classes!
      - Less sensitive to differences in growth shape between classes
    - LMR-LR test
      - Test of a solution with k-1 classes against a solution with k classes (e.g. 2 vs 1): low p-value indicates that solution k-1 should be rejected in favor of the solution with k classes.
    - Entropy
      - Measure of classification quality based on the individual class probabilities.
      - High values (closer to 1) indicate good classification.
- Examples with 2 classes:
  - [lcca\\_antit2.inp](#) (Nagin approach)
  - [lghm\\_antit2.inp](#) (with equal variances across classes)
  - [lghm\\_antit2free.inp](#) (with free variances across classes)

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**With 4+ WAVES of data**  
**Latent Growth Mixture Modeling (LGMM)**  
**Latent Class Growth Analysis (LCGA)**

Antisocial data: fit statistics

k	LCGA			LGMM		
	BIC	entropy	pLMRT	BIC	entropy	pLMRT
2l	4707.35	.97	.000	4653.78	.95	.002
3l	4681.69	.80	.030	4635.85	.79	.332
4l	4685.03	.81	.248	4625.88	.83	.154
2c	4533.67	.97	.000	4506.76	.99	.000
3c	4497.46	.82	.045	4487.26	.83	.411
4c	4476.20	.82	.014	4475.70	.85	.230
5c	4462.39	.83	.006			
6c	4460.83	.83	.426			

- General measurement and design issues
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  - LTA
- Exercise !

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- General measurement and design issues
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**With 4+ WAVES of data**

**Latent Growth Mixture Modeling (LGMM)**

**Latent Class Growth Analysis (LCGA)**

Antisocial data: Best solution: 5 classes, LCGA, curvilinear

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- Exercise !

**With 4+ WAVES of data**

**Latent Growth Mixture Modeling (LGMM)**

Antisocial data: Best solution: lcga\_anti5c.dat

id	observed	prob	class
1,000	2,300	1,000	*
1,000	1,000	0,000	0,000
1,000	1,000	0,000	1,000
1,000	1,000	0,000	2,000
1,000	1,000	0,000	3,000
1,000	1,000	0,000	4,000
1,000	1,000	0,000	5,000
1,000	1,000	0,000	6,000
1,000	1,000	0,000	7,000
1,000	1,000	0,000	8,000
1,000	1,000	0,000	9,000
1,000	1,000	0,000	10,000
1,000	1,000	0,000	11,000
1,000	1,000	0,000	12,000
1,000	1,000	0,000	13,000
1,000	1,000	0,000	14,000
1,000	1,000	0,000	15,000
1,000	1,000	0,000	16,000
1,000	1,000	0,000	17,000
1,000	1,000	0,000	18,000
1,000	1,000	0,000	19,000
1,000	1,000	0,000	20,000
1,000	1,000	0,000	21,000
1,000	1,000	0,000	22,000
1,000	1,000	0,000	23,000
1,000	1,000	0,000	24,000
1,000	1,000	0,000	25,000
1,000	1,000	0,000	26,000
1,000	1,000	0,000	27,000
1,000	1,000	0,000	28,000
1,000	1,000	0,000	29,000
1,000	1,000	0,000	30,000
1,000	1,000	0,000	31,000
1,000	1,000	0,000	32,000
1,000	1,000	0,000	33,000
1,000	1,000	0,000	34,000
1,000	1,000	0,000	35,000
1,000	1,000	0,000	36,000
1,000	1,000	0,000	37,000
1,000	1,000	0,000	38,000
1,000	1,000	0,000	39,000
1,000	1,000	0,000	40,000
1,000	1,000	0,000	41,000
1,000	1,000	0,000	42,000
1,000	1,000	0,000	43,000
1,000	1,000	0,000	44,000
1,000	1,000	0,000	45,000
1,000	1,000	0,000	46,000
1,000	1,000	0,000	47,000
1,000	1,000	0,000	48,000
1,000	1,000	0,000	49,000
1,000	1,000	0,000	50,000
1,000	1,000	0,000	51,000
1,000	1,000	0,000	52,000
1,000	1,000	0,000	53,000
1,000	1,000	0,000	54,000
1,000	1,000	0,000	55,000
1,000	1,000	0,000	56,000
1,000	1,000	0,000	57,000
1,000	1,000	0,000	58,000
1,000	1,000	0,000	59,000
1,000	1,000	0,000	60,000
1,000	1,000	0,000	61,000
1,000	1,000	0,000	62,000
1,000	1,000	0,000	63,000
1,000	1,000	0,000	64,000
1,000	1,000	0,000	65,000
1,000	1,000	0,000	66,000
1,000	1,000	0,000	67,000
1,000	1,000	0,000	68,000
1,000	1,000	0,000	69,000
1,000	1,000	0,000	70,000
1,000	1,000	0,000	71,000
1,000	1,000	0,000	72,000
1,000	1,000	0,000	73,000
1,000	1,000	0,000	74,000
1,000	1,000	0,000	75,000
1,000	1,000	0,000	76,000
1,000	1,000	0,000	77,000
1,000	1,000	0,000	78,000
1,000	1,000	0,000	79,000
1,000	1,000	0,000	80,000
1,000	1,000	0,000	81,000
1,000	1,000	0,000	82,000
1,000	1,000	0,000	83,000
1,000	1,000	0,000	84,000
1,000	1,000	0,000	85,000
1,000	1,000	0,000	86,000
1,000	1,000	0,000	87,000
1,000	1,000	0,000	88,000
1,000	1,000	0,000	89,000
1,000	1,000	0,000	90,000
1,000	1,000	0,000	91,000
1,000	1,000	0,000	92,000
1,000	1,000	0,000	93,000
1,000	1,000	0,000	94,000
1,000	1,000	0,000	95,000
1,000	1,000	0,000	96,000
1,000	1,000	0,000	97,000
1,000	1,000	0,000	98,000
1,000	1,000	0,000	99,000
1,000	1,000	0,000	100,000

Observed scores      Individual estimated class probabilities      Classification

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- Exercise !

**With 3/4+ WAVES of data**

**Latent Transition Analysis (LTA)**

(Kaplan, 2008; Meeus et al., 2010)

- A longitudinal extension of LCA or LPA
  - first, uses **class-specific parameters** (the continuous/categorical observed multidimensional scores) as measurement parameters (- LCA or cluster analysis)
    - invariant across time!
  - and, uses **class probabilities as structural parameters** to estimate the number of participants in each of the classes
  - then using **latent transition probabilities to calculate patterns of stability and change over time** in the movement or transition between classes (~ mover-stayer model)

→ An ideal model for testing typological or person-oriented developmental theories!

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With 3/4+ WAVES of data  
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Example: data on parenting across three waves

- 659 adolescents, measured 3 times: 13, 15 and 17 years
- psychological control, support/warmth, firm control (continuous)
- scores standardized (z) to ease interpretation

hypotheses: at least 4 latent classes (parenting styles) an gradually better parenting from 13 (peak of puberty years; reactive parenting) to 17 years

- estimated using Robust Maximum Likelihood estimation
- models with different # latent classes fitted and compared
- decision based on BIC, entropy, and interpretability

[lta parenting4.inp](#)

k	BIC	entropy
3	15308.59	.93
4	15016.72	.92
5	14982.35	.90
6	15324.43	.92

Exercise !

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With 3/4+ WAVES of data  
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Selected output k = 5 solution

- Measurement part + latent class probabilities

	Psychological Control	Support	Firm Control	13	15	17
Neglecting	-0.38	-0.11	-0.54	49%	29%	30%
Permissive	-0.67	1.21	0.64	24%	18%	19%
Rejecting	0.34	-1.17	-1.19	10%	8%	9%
Controlling	1.00	-0.62	-0.07	15%	16%	16%
Democratic	-1.66	1.36	1.23	1%	28%	26%

Exercise !

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With 3/4+ WAVES of data  
**Latent Transition Analysis (LTA)**  
(Kaplan, 2008; Meeus et al., 2010)

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Selected output k = 5 solution

- Transition probabilities

	Neglecting	Permissive	Rejecting	Controlling	Democratic
Neglecting 1	.574	.020	.000	.006	.400
Permissive 1	.000	.728	.000	.008	.264
Rejecting 1	.090	.000	.813	.000	.097
Controlling 1	.000	.000	.000	.974	.026
Democratic 1	.000	.000	.000	.272	.728
Neglecting 2	.971	.003	.000	.000	.026
Permissive 2	.000	.894	.000	.004	.102
Rejecting 2	.027	.000	.953	.000	.021
Controlling 2	.007	.000	.006	.870	.117
Democratic 2	.033	.094	.026	.086	.761

Exercise !

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• General measurement and design issues

- Measurement
- Time & Intervals
- Differential growth
- Missing values

• Classic methods and disadvantages

- Difference score
- Repeated ANOVA
- Autoregression
- Cross-lagged models

• New(er) methods

- LCM
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• Exercise !

### To conclude

• Since two decades, we have interesting new methods to analyze change and development!

• *Mplus* provides a powerful tool to analyze change and development, and is constantly improving!

• And, as said before...

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- Exercise !
  1. Check the direction of effects (using a cross-lagged model) between GPA and antisocial behavior, using data of Times 1 and 3. Check whether results are the same for boys and girls.  
DATA are SEMDATA.DAT; software = Mplus 8.0
  2. Estimate a LGCM of GPA, using the FIML approach for missing data. Check models with linear and curvilinear change. Interpret the parameters that are found.  
DATA are SEMDATA.DAT; software = Mplus 8.0
  3. Find the optimal LCGA/LGMM solution of the GPA data. Explain why this solution was chosen and interpret the different classes.  
DATA are SEMDATA.DAT; software = Mplus 7.3
  4. Evaluate the effect of mother support on development of GPA, using a conditional growth model and FIML  
DATA are SEMDATA.DAT; software = Mplus 8.0
  5. Test the multivariate LGCM of ANTI & GPA, using the FIML approach for missing data. Search for the best fitting model. Interpret the all the estimated parameters in this model.
    - Setup and do the analyses using Mplus!
    - Ask for help while doing the analyses!
    - Present the results to the audience, using a single or two slides and explain the effects in words!

## Informative websites

- [www.statmodel.com](http://www.statmodel.com): the Mplus site!
- <http://davidakenny.net/cm/causalm.htm>: great SEM page!
- <https://stats.idre.ucla.edu/mplus/>: online examples and videos on Mplus
- <http://users.ugent.be/~wbeyers/workshop/index.html>: the website for this workshop!

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### **Defining time and choosing intervals**

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### **Missing data and how to handle them**

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### **Latent Class Growth Analysis (LCGA)**

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### **Latent Growth Mixture Modeling (LGMM)**

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