The role of phonological and visual working memory in complex arithmetic for Chinese and Canadian adults

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Abstract

Two experiments were conducted to test cultural differences in the role of phonological and visual working memory in complex arithmetic. Canadian and Chinese students solved complex subtraction problems (e.g., 85 – 27; Experiment 1) and complex multiplication problems (e.g., 6 x 13; Experiment 2) under phonological and visual working memory loads. Problem complexity (i.e., borrow or carry operations) and presentation format (i.e., horizontal vs. vertical) were also manipulated. The results showed that Chinese and Canadians relied on both phonological and visual working memory resources when solving complex subtraction and multiplication problems. Selective involvement of phonological and visual working memory as a function of operation (Lee & Kang, 2002) or presentation format (Trbovich & LeFevre, 2003) was only found for Chinese and not for Canadians, calling into question the generalizability of these findings across arithmetic operations and cultural groups.

The role of phonological and visual working memory in complex arithmetic for Chinese and Canadian adults

Mental arithmetic is a skill that people use every day. Some arithmetic problems, such as 3 + 2 or 8 - 4 are relatively easy to solve. As problems become more complex, however, such as 45 + 29 or 78 - 15, greater mental effort is required and a variety of mental processes are recruited. In the present research, we explored the role of phonological and visual working memory processes in the solution of complex subtraction and multiplication problems. Although it is generally acknowledged that working memory plays a significant role in arithmetic problem solving (DeStefano & LeFevre, 2004), the involvement of working memory resources seems to depend on various factors such as presentation format (horizontal vs. vertical), operation (subtraction vs. multiplication), and problem complexity (easy vs. difficult). One goal of the present study was to determine whether phonological and visual working memory resources were differently invoked depending on these factors.

In addition to the role of problem-based factors in arithmetic, the involvement of working memory may vary with educational experiences and arithmetic skill (Imbo & LeFevre, in press). Assessment of working memory demands of specific operations or particular formats has usually been done only for relatively homogenous groups, however, and thus generalizability of the results may be limited. To explore this issue, in the present research we tested participants from two different cultures: Chinese-educated Asians and Canadian-educated North Americans. In the domain of simple arithmetic, Asians are more skilled than North Americans (e.g., Campbell & Xue, 2001; LeFevre & Liu, 1997), and this advantage may exist even before children enter elementary school

(Siegler & Mu, 2008). Thus, our second goal in the present research was to evaluate the hypothesis that cultural differences in solution processes and hence in working memory demands may also be found in the domain of complex arithmetic.

The working memory model of Baddeley and Hitch (1974, Baddeley, 2000) has proven to be useful in research on working memory and mental arithmetic. According to this model, four components constitute working memory: the central executive, the phonological loop, the visual-spatial sketchpad, and the episodic buffer. The central executive is a modality-free, limited-capacity system that includes control processes, monitoring, response selection, planning, and sequencing. The phonological loop and the visual-spatial sketchpad store phonological and visual-spatial information, respectively. The episodic buffer combines temporary working memory information with long term memory information.

In the present study we investigated the involvement of two working memory components, the phonological loop and the visual-spatial sketchpad, in two arithmetic operations, subtraction and multiplication. We explored the extent to which previously obtained results regarding working memory and arithmetic are generalizable across groups differing in culture, arithmetic skill, and educational history. Our examination of cultural differences was in part motivated by the observation that the role of working memory components has rarely been examined for the same operations across cultures. For example, there is some support for a role of the phonological loop in subtraction and multiplication but it is culture specific in that effects have been observed for Germans solving multiplication problems (Seitz & Schuman-Hengsteler, 2000, 2002), for Americans solving subtraction problems (Seyler, Kirk, & Ashcraft, 2003), and for

Belgians solving multiplication and subtraction problems (Imbo, Vandierendonck, & Vergauwe, 2007). There are no cross-cultural comparisons and no published accounts of Asian-educated adults solving complex arithmetic problems. Such comparisons would be of interest because two possible roles for the phonological loop in multiplication have been proposed and these roles may vary across cultures as well as across problem complexity.

For simple multiplication, facts may be stored in an internal phonological code (Dehaene, 1992, 1997; Cohen & Dehaene, 2000; Cohen et al., 2000; Dehaene & Cohen, 1995, 1997; Lee & Kang, 2002). Because Asian students practice multiplication using rote memorization and verbal repetition, the role of phonological codes may be greater for Asian than for Canadian students (Campbell & Xue, 2001; LeFevre & Liu, 1997). Thus, we predicted that for multiplication, Chinese-educated participants might need more phonological resources than Canadian-educated participants.

In contrast, the role of the phonological loop in complex problems, both multiplication and subtraction, may be to store intermediate solutions (Ashcraft, 1995). For example, solving 56 x 4 involves the subproblems 4 x 6, 4 x 50, and 24 + 200. The intermediate products 24 and 200 may be stored in the phonological loop. Similarly, for the problem 46 – 19, the phonological loop may be used to maintain intermediate components of the solution, such as the borrowing of 10 from 40 and the unit solution 7 while the decade value is being processed. Thus, we predicted that both subtraction and multiplication would involve the phonological loop because of the possible storage function and that this would be true for both Chinese- and Canadian-educated participants. Overall therefore, the use of a phonological code in multiplication seems

more likely for Chinese- than for Canadian-educated individuals, because the former rely more heavily on rote memorization of multiplication facts (e.g., Campbell & Xue, 2001; LeFevre & Liu, 1997) whereas both groups are likely to use the phonological loop for storage of intermediate solutions. Thus, cross-cultural comparisons will address the question of whether effects of working memory can be linked to differences in how arithmetic facts are stored and processed.

In contrast, there is less research supporting a role for visual-spatial working memory in complex arithmetic and therefore few specific predictions. Lee and Kang (2002) found that a visual-spatial task interfered with performance on simple subtraction but not multiplication problems. For simple subtraction (and possibly addition), some researchers have proposed that activation of an internal magnitude code or number line representation occurs (e.g., Dehaene, 1992, 1997; Dehaene & Cohen, 1995, 1997) and thus engages visual or spatial codes in working memory. Little support for this proposal has been found for simple addition or subtraction, but no researchers other than Lee and Kang have evaluated the hypothesis within a working memory framework.

For complex arithmetic, significant visual load effects have only been observed by Trbovich and LeFevre (2003). In their study, Canadian-educated participants solved horizontally or vertically presented 1-digit + 2-digit addition problems (e.g., 8 + 43) under phonological and visual working memory loads. Trbovich and LeFevre found decrements in performance with both types of load, but the phonological load affected horizontally presented problems more whereas a visual load affected vertically presented problems more. These results were interpreted in the light of the participants' strategy choices. Trbovich and LeFevre hypothesized that vertically presented problems are likely

to activate the solution algorithm used in pencil-and-paper calculations (that is processing each column of numbers sequentially), which may invoke more visual than phonological working memory resources (see also Heathcote, 1994). Horizontally presented problems, in contrast, activate decomposition strategies (e.g., solving 45 + 9 as 45 + 5 + 4), which may be more likely to involve verbal codes, and thus involve phonological working memory resources (see also Shanahan, 2009).

In sum, Trbovich and LeFevre's results indicate that visual codes are most strongly activated for problems in vertical format; in the present study we tested whether this would be true for other operations than addition. Consistent with Trbovich and LeFevre's overall results, we predicted that both subtraction and multiplication would involve visual working memory. Complex arithmetic may routinely require visual working memory when the problems are displayed visually (vs. presented auditorily; Deslauriers, Ouellete, Barnes, & LeFevre, 2008; cf. Noël, Désert, Aubrun, & Seron, 2001). Subtraction may further invoke visual working memory processes because it is likely to activate an internal magnitude code. In agreement with Trbovich and LeFevre's format effects, we also predicted larger visual load effects for vertically than for horizontally presented problems. The inclusion of separate groups of participants educated in Canada and China allowed us to test if the interaction between working memory component (phonological vs. visual-spatial) and presentation format (horizontal vs. vertical) is universally true across cultures.

The involvement of working memory may also depend on problem complexity. In complex arithmetic, problem complexity is generally based on the number or difficulty of carry or borrow operations that have to be performed. Carrying is needed when the sum

or the product of the units is larger than 10, which means that an amount has to be carried from the units to the tens (e.g., 56 + 28, 6×24). Borrowing is needed when there is a shortfall (e.g., 52 - 17), resulting in a borrow operation from the tens to the units. Although evidence for the role of the central executive in carrying and borrowing is very strong (Ashcraft & Kirk, 2001; Fürst & Hitch, 2000; Imbo et al., 2007a,b; Seitz & Schumann-Hengsteler, 2002), the involvement of phonological and visual-spatial working memory resources in these processes is still debated. Some researchers did observe significant phonological working memory involvement in carrying and borrowing for Dutch- and German-educated adults (e.g., Imbo et al., 2007a,b; Seitz & Schumann-Hengsteler, 2000, 2002), whereas others did not observe such effects in British- and Canadian-educated adults (e.g., Logie et al., 1994; Fürst & Hitch, 2000; Trbovich & LeFevre, 2003). Evidence for a role of the visual-spatial sketchpad in carrying or borrowing has not been found in multi-digit arithmetic for British-, French-, or Canadian-educated adults (Logie et al., 1994; Noël et al., 2001; Trbovich & LeFevre, 2003).

In summary, in the present research we investigated the role of phonological and visual working memory as a function of presentation format (horizontal vs. vertical), problem complexity (easy vs. difficult), and operation (subtraction vs. multiplication). We hypothesized that both subtraction and multiplication would be affected by a phonological working memory load, because both operations involve retention of intermediate solutions (Noël et al., 2000; Trbovich & LeFevre, 2003). Similarly, we expected both subtraction and multiplication to be affected by a visual memory load (Deslauriers et al., 2008; Trbovich & LeFevre, 2003) although the effect may be greater

for subtraction on the view that solution of simple subtraction problems involves internal magnitude or number line representations (Lee & Kang, 2002). We also hypothesized that the decrements in performance would be greater for horizontally presented problems under a phonological load and for vertically presented problems under a visual load (Trbovich & LeFevre, 2003), to the extent that these orientations enhance or exacerbate the activation of the respective working memory loads.

Last but not least, the inclusion of Chinese and Canadian participants allowed us to test to what extent these results are generalizable across culture. Indeed, the respective interactions between working memory load and presentation format (Trbovich & LeFevre, 2003) and between working memory load and operation (Lee & Kang, 2002) have never been tested across cultures; it is thus perfectly possible that they are not universal. We expected the Chinese-educated participants to be more skilled at arithmetic than the Canadians and thus to show smaller effects of problem complexity. Chinese participants were also expected to show additional effects of phonological load on multiplication problems because they rely heavily on rote verbal memory to access component facts (LeFevre & Liu, 1997). However, we had no reason to predict differential patterns of working memory loads for subtraction problems across cultures.

Experiment 1

Method

Participants

Sixty-five participants were recruited for the present experiment. Twenty-nine (14 men and 15 women; mean age 21 years) were native English-speaking university students who had received their education in Canada. Thirty-six (14 men and 22 women; mean

age 24 years) were native Chinese-speaking students who had received their education in China but were currently living and studying in Canada. Their first language was Chinese and their second language was English. Everyone responded in English¹. Thirty-nine individuals participated to fulfill a course requirement and twenty-six were paid 12 Canadian dollars.

Materials

Subtraction task. Three sets of 20 subtraction problems were constructed, resulting in a total of 60 different problems. Each set was presented twice to each participant, that is, once in horizontal presentation and once in vertical presentation. The order of the three sets and the combination of the set with the working memory load conditions were counterbalanced. All problems consisted of two two-digit numbers that had two-digit answers (e.g., 85 - 27). Two types of problems were excluded: (a) problems involving a 0 in the units (e.g., 30 - 12; 32 - 10), or in the remainder (e.g., 46 - 26), and (b) problems involving a 9 in the units (e.g., 69 - 25 or 73 - 29), or in the remainder (e.g., 56-27). In order to exclude answer-size effects, the correct remainders of each set were equally distributed among the 30s, the 40s, the 50s, the 60s, and the 70s (i.e., four problems per type). Half of the problems involved a borrow operation from the tens to the units (e.g., 61 - 18; hard problems) whereas the other half did not (e.g., 74 - 32; easy problems). The size of the remainder was equal for no-borrow problems and one-borrow problems. We also controlled for the even/uneven status of the correct remainder (i.e., half of the remainders were even; the other half were uneven).

Phonological secondary task. In this task, letter strings of 4 consonants (e.g., TKXL) were read aloud by the experimenter. The participant had to retain these letters

and repeat them aloud after three subtraction problems². Following the response of the participant, the experimenter presented a new 4-letter string. For each correct letter that was remembered in its correct position, participants gained one point. The maximum score on each trial was 4 points (i.e., 100% correct). This task has been used previously in research on mental arithmetic (e.g., Imbo & Vandierendonck, 2007a,b), in which it has been shown that retaining letters only interferes with phonologically based calculation strategies (such as transformation and counting) but not with direct memory retrieval. The letter task was also tested individually (i.e., without the concurrent solving of arithmetic problems) for 2 minutes. In this secondary-task-only condition, an interval of 15 seconds was used between the presentation of the 4-letter string and the question to repeat the letters.

Visual secondary task. The visual memory load consisted of a pattern of four asterisks arranged in a 4 x 4 array. A list with 20 different patterns of four asterisks each was constructed. None of the asterisk patterns formed recognizable lines, figures, objects, or letters, to discourage the participants from using a verbal label as a memory aid. On each trial, a pattern was selected randomly and presented on the screen. The participant had to retain the pattern and reproduce it after three subtraction problems. For reproduction, the participant had to click with the mouse in the four appropriate grid locations (indicated by squares). Following the response of the participant, a new four-asterisk pattern was presented. For each star that was reproduced on its correct position, participants gained one point. The maximum score on each trial was 4 points (i.e., 100% correct). This task has been used previously in research on mental arithmetic (e.g., Trbovich & LeFevre, 2003) and word naming (e.g., Herdman & Beckett, 1996), and has

been shown to require the maintenance of visual codes and to be relatively free of phonological operations (Hellige, Cox, & Litvak, 1979). The star task was also performed alone (i.e., without the concurrent solving of arithmetic problems) for 2 minutes. The secondary-task-only execution of the phonological task and the visual task took place just before the execution of the primary task in combination with the respective secondary task. This ordering permitted the participants to get used to the secondary-task execution.

French Kit. After the complex-arithmetic experiment, all participants completed a portion of a paper-and-pencil test of arithmetic skill, the French Kit (French, Ekstrom, & Price, 1963). The test consisted of two subtests, one page with complex addition problems and one page with complex subtraction and multiplication problems.

Participants were given 2 minutes per page, and were instructed to solve the problems as fast and accurately as possible. The correct answers on both subtests were summed to yield a total score of arithmetic skill.

Procedure

Each participant was tested individually by the same experimenter. The experiment took place in a quiet room and lasted for approximately 1 hour. All participants solved 20 subtraction problems in each of the six conditions defined by the 2 (Presentation format: horizontal, vertical) x 3 (Working memory load: no load, phonological, visual) design. For half of the participants, the experiment started with the horizontal presentation format; for the other half, the experiment started with the vertical presentation format. The order of the working memory loads was randomized across participants.

A trial started with a fixation point for 500 ms, after which the subtraction

problem was presented in the center of the screen. The problem remained on screen until the participant responded. Timing began when the stimulus appeared and ended when the response triggered the sound-activated relay. To enable this sound-activated relay, participants wore a microphone that was activated when they spoke their answer aloud. This microphone was connected to a software clock accurate to 1 millisecond. On each trial, feedback was presented to the participants, a green 'Correct' when their answer was correct, and a red 'Incorrect' when it was not.

Results

In total, 2.8% of the trials were spoiled due to failures of the sound-activated relay. All data were analyzed on the basis of the multivariate general linear model; and all reported results were significant at p < .05, unless mentioned otherwise. Two Canadian participants did not solve any borrow problems correctly and were removed from all further analyses. Thus, the final sample included twenty-seven Canadians and thirty-six Chinese. An analysis of French Kit scores confirmed that the Chinese had a substantially higher level of arithmetic skill than the Canadians (54 vs. 34), F(1,61) = 38.04, MSe = 166, $\eta_p^2 = 0.38$.

Secondary Task Performance

Percentage correct on each secondary task was analyzed separately in an ANOVA with Culture (Canadian vs. Chinese) as between-subject factor and repeated measures on Condition (single, dual-horizontal, dual-vertical; see Table 1).

Phonological Memory. Accuracy varied with Condition, F(2,60) = 40.62, MSe = 130, $\eta_p^2 = 0.40$. Participants were more accurate in the single-task condition (79%) than in the dual-horizontal (64%) and the dual-vertical conditions (63%), F(1,61) = 56.57 and

F(1,61) = 65.98. Accuracies on the phonological task did not differ across dual-horizontal and dual-vertical conditions (F<1). No other effects were significant (Fs<1).

Visual Memory. Accuracy varied with Condition, F(2,60) = 148.55, MSe = 126, $\eta_p^2 = 0.71$. Participants were more accurate in the single-task condition (97% correct) than in the dual-horizontal condition (74%), F(1,61) = 141.63, and tended to be more accurate in the latter condition than in the dual-vertical condition (70% correct), F(1,61) = 3.45, p = .06. Further planned comparisons showed that Canadians' accuracies did not differ across dual-horizontal and dual-vertical conditions (71% vs. 72%; F<1). However, Chinese were significantly less accurate in the dual-vertical (69% correct) than in the dual-horizontal condition (76% correct), F(1,61) = 5.95, which indicates that the Chinese need more visual working memory resources to solve vertically presented subtraction problems than to solve horizontally presented subtraction problems. This result extends the conclusion of Trbovich and LeFevre (2003), who observed that visual working memory resources were more used for vertically- than for horizontally-presented addition problems.

Subtraction

Latencies. Latencies on correctly solved problems were analyzed in a 2 (Culture: Canadian vs. Chinese) x 2 (Presentation format: horizontal vs. vertical) x 3 (Working memory load: control vs. phonological vs. visual) x 2 (Problem complexity: easy vs. difficult) ANOVA with repeated measures on the last three factors (see Table 2). People were faster on vertically- than on horizontally-presented problems (3.6. vs. 4.0 s), F(1,61) = 27.42, MSe = 909675, $\eta_p^2 = 0.31$, and faster on easy than on hard problems (2.9 vs. 4.7 s), F(1,61) = 115.82, MSe = 5477819, $\eta_p^2 = 0.66$. The main effect of Working memory

load, F(2,60) = 12.13, MSe = 966070, $\eta_p^2 = 0.17$, showed that people were faster in the no-load condition (3.5 s) than under a phonological load (3.9 s), F(1,61) = 17.11 or a visual load (3.9 s), F(1,61) = 21.12. They were equally slow in both working memory load conditions (F<1). As expected, Chinese (2.9 s) were significantly faster than Canadians (4.6 s), F(1,61) = 24.29, MSe = 22817190, $\eta_p^2 = 0.28$. Culture further interacted with Problem complexity, F(1,61) = 11.39, MSe = 5477819, $\eta_p^2 = 0.16$. The problem complexity effect was larger in Canadians (2.4 s) than in Chinese (1.3s). The Culture x Presentation format and Culture x Working memory load interactions did not reach significance (both ps > .25).

Errors. Percentages of errors were analyzed in a similar 2 x 2 x 3 x 2 ANOVA (see Table 3). The main effects of Problem complexity and Culture were significant, F(1,60) = 50.25, MSe = 410, $\eta_p^2 = 0.46$, and F(1,60) = 6.14, MSe = 561, $\eta_p^2 = 0.09$, respectively. Error rates were higher on difficult problems (16.7%) than on easy problems (6.0%) and higher in Canadians (13.5%) than in Chinese (9.2%). Culture and Problem complexity also interacted, F(1,60) = 5.09, MSe = 410, $\eta_p^2 = 0.08$. The problem complexity effect was larger in Canadians (14.1%) than in Chinese (7.3%). The Culture x Presentation format and Culture x Working memory load interactions did not reach significance (both ps > .55).

Discussion

The results of the present experiment showed that both phonological and visual working memory resources are used when people solve multi-digit subtraction problems. Both Canadian and Chinese participants showed significant decrements in solution times in the dual-task conditions. In accord with previous findings about cultural differences,

Chinese participants performed better on the subtraction problems than the Canadian participants: they solved the problems more quickly and more accurately, and they were less affected by problem complexity (Campbell & Xue, 2001; Imbo & LeFevre, in press). However, only the Chinese participants showed differential decrements related to presentation format (cf. Trbovich & LeFevre, 2003). They made more errors on the visual secondary task when solving vertically presented problems than when solving horizontally presented problems. This result shows that Trbovich and LeFevre's results may not be generalizable across operations or across cultural groups.

Experiment 2 was similar to Experiment 1, except that multiplication problems were tested instead of subtraction problems. The predictions for multiplication were somewhat different than for subtraction. In particular, Lee and Kang (2002) reported that visual-spatial working memory resources were important for subtraction (as was found in Experiment 1), whereas phonological resources were important for multiplication. Thus, we might expect an interaction such that phonological loads affect multiplication more than visual loads. Results for non-Asian groups have suggested that complex multiplications require phonological working memory and executive resources, but no studies (other than Lee & Kang) have used visual-spatial working memory loads with multiplication problems. Thus, the specificity of working memory components in relation to multiplication has not been tested across cultures for complex problems.

Experiment 2

Method

Participants

Sixty-seven participants were recruited for the present experiment. Thirty (16 men

and 14 women; mean age 24 years) were native English-speaking university students who had received their education in Canada. Thirty-seven (14 men and 23 women; mean age 23 years) were Chinese-speaking university students who had received their education in China but were currently living and studying in Canada. Their first language was Chinese and their second language was English. Everyone responded in English. Fifty individuals participated for course credit and seventeen were paid 12 Canadian dollars.

Procedure and Tasks

The set of 20 multiplication problems consisted of one-digit \times two-digit problems that met the following restrictions: (a) the two-digit number was not a decade (e.g., 3×50), (b) the correct product was not a decade (e.g., 5×16), and (c) the one-digit number was not 1, 2, or 9 (e.g., 2×14). Further, all correct products were larger than 30 and smaller than 90. In this set of twenty problems, there were three problems without a carry operation (e.g., 4×12), nine problems with a carry value of 1 (e.g., 4×14), six problems with a carry value of 2 (e.g., 4×16), and two problems with a carry value of 3 (e.g., 4×18). Problems with a carry value of 0 or 1 were coded as easy; problems with a carry value of 2 or 3 were coded as difficult. The same set of problems was presented six times to each participant. The procedure, the secondary tasks and the French Kit were identical to the previous experiments.

Results

In total, 2.8% of the trials were spoiled due to failures of the sound-activated relay. All data were analyzed on the basis of the multivariate general linear model; and all reported results were significant at p < .05, unless otherwise indicated. An analysis of French Kit scores confirmed that the Chinese had a higher level of arithmetic skill than

the Canadians (48 vs. 30), F(1,65) = 38.25, MSe = 139, $\eta_p^2 = 0.37$. Secondary Task Performance

Percentage correct on each secondary task was analyzed separately in an ANOVA with Culture (Canadian vs. Chinese) as a between-subject factor and repeated measures on Condition (single, dual-horizontal, dual-vertical; see Table 1).

Phonological memory. The main effect of Condition was significant, F(2,64) = 70.46, MSe = 151, $\eta_p^2 = 0.52$. Participants were more accurate in the single-task condition (80% correct) than in the dual-horizontal condition (62% correct) and the dual-vertical condition (64% correct), F(1,65) = 90.00 and F(1,65) = 76.78. Accuracies on the phonological task did not differ across dual-horizontal and dual-vertical conditions (F<1). The main effect of Culture and the interaction between Culture and Condition did not reach statistical significance (both Fs<1).

Visual memory. A similar ANOVA was conducted on the accuracies of the visual secondary task (see Table 1). The main effect of Condition was significant, F(2,64) = 91.14, MSe = 143, $\eta_p^2 = 0.59$. Participants were more accurate in the single-task condition (96% correct) than in the dual-horizontal condition (77% correct) and the dual-vertical condition (74% correct), F(1,65) = 88.37 and F(1,65) = 140.90. Accuracies on the visual task did not differ across dual-horizontal and dual-vertical conditions, F(1,65) = 2.38 (p = .13). The main effect of Culture and the interaction between Culture and Condition did not reach statistical significance (both Fs<1).

Multiplication

Latencies. Latencies on correctly solved problems were analyzed in a 2 (Culture: Canadian vs. Chinese) x 2 (Presentation format: horizontal vs. vertical) x 3 (Working

memory load: control vs. phonological vs. visual) x 2 (Problem complexity: easy vs. difficult) ANOVA with repeated measures on the last three factors (see Table 2). People responded faster on vertically- than on horizontally-presented problems (3.7 vs. 4.0 s), F(1,65) = 8.46, MSe = 1500118, $\eta_p^2 = 0.12$, and faster on easy problems (4.2 s) than on difficult problems (5.5 s), F(1,65) = 88.45, MSe = 2028826, $\eta_p^2 = 0.58$. The main effect of Working memory load, F(2,64) = 36.37, MSe = 710494, $\eta_p^2 = 0.36$, indicated that people were faster under no-load conditions (3.5 s) than under phonological load (4.1 s) or under visual load (4.0 s), F(1,65) = 48.81 and F(1,65) = 65.36. They were as slow under phonological load as under visual load, F<1. Chinese (2.9s) responded faster than Canadians (4.8s), F(1,65) = 26.63, MSe = 28673880, $\eta_p^2 = 0.29$. Culture further interacted with Problem complexity, F(1,65) = 12.75, MSe = 2028826, $\eta_p^2 = 0.16$. The problem complexity effect was larger in Canadians (1.3 s) than in Chinese (0.6 s). The Culture x Presentation format and Culture x Working memory load interactions did not reach significance (both ps > .20).

Errors. Percentages of errors were analyzed in a similar 2 x 2 x 3 x 2 ANOVA (see Table 3). The main effects of Problem complexity and Culture were significant, F(1,65) = 28.01, MSe = 282, $\eta_p^2 = 0.30$, and F(1,65) = 9.96, MSe = 555, $\eta_p^2 = 0.13$. Error rates were larger for difficult problems (13.8%) than for easy problems (7.4%), and larger in Canadians (13.2%) than in Chinese (8.0%). The interaction between Culture, Problem complexity, and Presentation format was significant, F(1,65) = 4.59, MSe = 127, $\eta_p^2 = 0.07$. The problem complexity effect was larger in Canadians than in Chinese for vertically presented problems (9.7% vs. 2.4%), F(1,65) = 7.01, but not for horizontally presented problems (6.8% vs. 6.2%), F<1. The interaction between Presentation format

and Working memory load was tested separately for each culture to evaluate the prediction that the Chinese would be more affected by a phonological working memory load than a visual load. As expected, no differential load effects were found for the Canadians. For the Chinese participants, however, the interaction was significant, F(1,36) = 4.67, $\eta_p^2 = 0.11$. For the Chinese participants, phonological load effects were significant for horizontally presented problems (3.4%), F(1,36) = 7.12, but not for vertically presented problems (1.9%); p = .15. Visual load effects, in contrast, tended to be significant for vertically presented problems (2.9%), F(1,36) = 3.26 (p = .07), but were not significant for horizontally presented problems (0.4%), F<1.

Discussion

The results of the present experiment showed that both phonological and visual working memory resources are used when people solve multi-digit multiplication problems. Solution times on the multiplication problems and performance on the load tasks showed significant decrements in the dual-task conditions. Chinese participants performed better on the multiplication problems than the Canadian participants: they solved the problems more quickly and more accurately, and they were less affected by problem complexity. As in Experiment 1, only the Chinese participants showed differential decrements related to presentation format. Patterns were different across experiments, however. In Experiment 2, Chinese-educated participants made more errors on the multiplication task under a phonological load in horizontal than in vertical format, whereas in Experiment 1, subtraction was more affected by a visual load. Hence, the results of both experiments indicate that the interaction between working memory resources (phonological vs. visuo-spatial) and presentation format (horizontal vs.

vertical) is not unconditionally valid. In the present research interactions were found for Chinese but not for Canadians in that Canadians showed decrements in performance for both operations, both presentation formats, and both types of working memory load. In the General Discussion, we interpret the current results in the light of previous studies (Lee & Kang, 2002; Trbovich & LeFevre, 2003) and explore the question of why results may not always be generalizable across arithmetic operations and cultural groups.

General Discussion

We conducted two experiments to investigate cultural differences in complex arithmetic, as well as their interaction with presentation format, working memory load, and problem complexity. As predicted, both Canadians and Chinese relied on phonological and visual working memory resources when solving complex arithmetic problems. Decrements occurred for both groups in subtraction and in multiplication. Differential working memory load effects as a function of presentation format (cf. Trbovich & LeFevre, 2003) and operation (cf. Lee & Kang, 2002) were only significant for Chinese, and not for Canadians, however. Chinese participants showed greater phonological load effects on multiplication problems in horizontal than in vertical format, consistent with the view that the horizontal format exacerbated the deleterious effect of the phonological load. Chinese participants also showed greater decrements on the visual load task for vertically presented subtractions than for horizontally presented subtractions, supporting the view that the vertical format exacerbated the effect of the visual load. Canadian, in contrast, showed decrements to both types of loads in both format conditions across operations.

The observation of significant working memory load effects in the Canadian

sample is in agreement with two earlier studies on Canadians' complex arithmetic performance: Imbo and LeFevre (in press) found phonological load effects and Trbovich and LeFevre (2003) found both visual and phonological load effects. Both studies only tested complex addition, however, so the present study extends these results to other operations by showing that Canadians need both phonological and visual working memory resources when solving complex subtractions and multiplications. Given the higher level of mathematical skill in Asian than in Canadian participants (Campbell & Xue, 2001; Imbo & LeFevre, in press; LeFevre & Liu, 1997; Siegler & Mu, 2008), we had anticipated that working memory load effects might be less in the Chinese than in the Canadians. However, Chinese-educated participants in the current research did slow down under phonological and visual working memory loads, even though other Chinese participants did not rely on executive working memory resources when solving complex addition problems (Imbo & LeFevre, in press). Hence, Chinese may not rely on the controlling or monitoring function of their working memory when solving complex additions, but they do rely on the storage capacity of their working memory when solving complex subtractions and multiplications. In sum, both Chinese and Canadian participants relied on phonological and visual working memory when solving complex subtractions and multiplications, suggesting that they maintained intermediate solutions in a verbal format and on a mental blackboard. How the mental blackboard maintains visual information and which specific role it plays in mental arithmetic are questions that should be addressed in future research.

We also observed some evidence for the link between working memory and presentation format (cf. Trbovich & LeFevre, 2003). Whereas Canadians did not show

differential load effects as a function of presentation format, Chinese did: in the subtraction experiment they relied more on visual memory for vertically- than for horizontally-presented problems, and in the multiplication experiment they relied more on phonological memory for horizontally- than for vertically-presented problems.

Trbovich and LeFevre (2003) found that addition problems in vertical format involved visual working memory to a greater degree whereas those in horizontal format involved phonological working memory. Thus, although aspects of the current results are in agreement with those of Trbovich and LeFevre (2003), the present results also show that one should be careful when generalizing effects of working memory load over operations or over cultural groups.

Differential load effects as a function of presentation format seem to be detected more easily in addition than in other, less practiced operations such as subtraction and multiplication. Obviously, performance measures such as response times and error rates are more variable for less practiced operations, and this variability may have obscured possible interactions. The variability is even greater in less-skilled participants, such as the Canadians in our study. The performance of the highly-skilled Chinese was more efficient (i.e., faster and less erroneous) and correspondingly less variable than that of the Canadians, which may have increased the chance of observing differential load effects in the former than in the latter.

Another explanation for the fact that differential load effects were culturally specific may be found in the different educational approaches in Asian and non-Asian cultures. In the Chinese education system, the multiplication tables are taught by using rhyming formulae, and involve extensive training in the form of drill and rote verbal

memory (Zhang & Zhou, 2003), accounting for the connection between the phonological loop and horizontally presented multiplication problems (cf. Experiment 2). Additions and subtractions, in contrast, are often taught by using the abacus (Cantlon & Brannon, 2007; Stigler, 1984), which relies on a vertical mental representation requiring visual working memory resources (cf. Experiment 1). Imaging studies indeed showed that the mental abacus operation is associated with enhanced activity in the brain areas relevant for visual-spatial information processing (e.g., Hanakawa et al., 2003; Wu et al., 2009). Hence, the distinct Chinese training regimens may lead to distinct mental processes and representations across operations.

Different educational approaches are common in North America than in China. First of all, North Americans are less thoroughly drilled and trained than are Asians. This lack of automaticity implies a greater use of executive working memory resources in North Americans than in Asians (cf. Imbo & LeFevre, in press). Further, the more exploratory approach to learning arithmetic favored in North American education may result in a greater variety in strategy use (cf. Campbell & Xue, 2001; LeFevre & Liu, 1997). Canadians' highly variable strategy use may increase the need for phonological and visual working memory resources, if the information has to be stored (as intermediate solutions) differentially across problems and operations. Hence, the specific functions of the phonological loop and the visual sketchpad may be more consistent for Chinese than for Canadians.

Also note that the differential load effects were only found in errors (i.e., secondary task errors in Experiment 1 and multiplication errors in Experiment 2).

Similarly, in Trbovich and LeFevre, differential effects of working memory load were

only found on error scores (combined across the secondary and arithmetic tasks). These patterns suggest that the role of working memory subsystems in complex arithmetic is more strongly connected to maintaining and accessing representations than to the speed with which the processing is implemented. This observation suggests that further research would be fruitful in exploring in more detail how working memory is involved in the problem solving process.

Finally, cultural differences in the problem complexity effect were observed as well. The Chinese were more proficient in solving carry and borrow problems than the Canadians. Cultural differences in problem solving have been shown in the domain of simple arithmetic (e.g., Campbell & Xue, 2001; LeFevre & Liu, 1997), and for one study, in complex arithmetic (Imbo & LeFevre, in press). Speed and accuracy scores are lower for Canadians than for Chinese – and these differences increase as problem complexity increases for both simple arithmetic (Campbell & Xue, 2001; LeFevre & Liu, 1997) and complex arithmetic (this study; see also Imbo & LeFevre, in press). Hence, the Chinese are not only generally more efficient; they are also specifically more efficient on the difficult carry and borrow problems, suggesting higher levels of competency in both declarative and procedural knowledge.

Despite the clear effect of problem complexity in both experiments, borrowing and carrying did not directly tax phonological or visual working memory. Research on the possible role of phonological working memory resources in carrying and borrowing has yielded equivocal results. Some researchers did observe significant phonological load effects that varied with problem complexity (e.g., Imbo et al., 2007a,b; Seitz & Schumann-Hengsteler, 2000, 2002), whereas others did not (e.g., Logie et al., 1994; Fürst

& Hitch, 2000; Trbovich & LeFevre, 2003). One intriguing possibility is that the language of the participants may influence whether phonological resources are implicated in arithmetic solutions. The only studies that observed phonological load effects on carrying and borrowing have been conducted on Dutch- (Imbo et al., 2007a,b) or German-speaking participants (Seitz & Schumann-Hengsteler, 2000, 2002). The number language of these Germanic languages is different from that of English or Asian languages (i.e., 45 is pronounced as "five and forty"). This inverse order of pronunciation (relative to the Arabic digit form) may require extra phonological working memory involvement (see Brysbaert, Fias, & Noël, 1998); a hypothesis that needs to be tested in further studies. The absence of visual load effects on carrying or borrowing is in agreement with the – very few – studies on this topic (Logie et al., 1994; Noël et al., 2001; Trbovich & LeFevre, 2003), and indicates that the visual-spatial sketchpad is not involved in carrying or borrowing.

In summary, both Canadians and Chinese relied on phonological and visual working memory resources when solving complex subtraction and multiplication problems. Although the Chinese were more efficient than the Canadians, the involvement of phonological and visual working memory recourses was comparable. However, differential working memory load effects were obtained only for Chinese and not for Canadians. More specifically, Chinese showed a greater role for the phonological loop in horizontally- than in vertically-presented multiplication problems (Experiment 2) and a greater role for the visual-spatial sketchpad in vertically- than in horizontally-presented subtraction problems (Experiment 1). Conclusions from earlier experiments conducted within a single culture can thus not necessarily be generalized. Inter-cultural studies have

a double advantage: they test for differences *between* cultures; and they also test if widely accepted conclusions can be generalized *over* cultures. Thus, more systematic comparisons of performance across different cultural groups and different arithmetic operations are likely to yield useful information for theories of how numerical information is processed and represented.

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Footnotes

- Although having to respond in their second language might have been a small
 disadvantage for the Chinese, the results show that they nevertheless performed better
 than the Canadians. Thus, although a possible effect of language of testing cannot be
 discounted in the current research, this issue seems unlikely to have compromised the
 main conclusions.
- 2. In order to have seven series of three arithmetic problems each, one subtraction problem (Experiment 1) and one multiplication problem (Experiment 2) was repeated. This problem was chosen randomly from the set of 20 problems.

Table 1

Mean accuracies and standard errors on the phonological and visual secondary tasks.

		Canadian		Chinese		
Task	Load Condition	M	SE	M	SE	
Subtraction (Experi						
Phonological task	Single	79.2	0.6	79.6	0.5	
	Dual-horizontal	65.2	3.1	62.9	2.7	
	Dual-vertical	64.1	3.0	61.8	2.6	
Visual task	Single	97.0	0.8	96.0	0.6	
	Dual-horizontal	70.2	3.0	76.0	2.5	
	Dual-vertical	70.8	2.8	68.8	2.5	
Multiplication (Experiment 2)						
Phonological task	Single	80.3	0.2	80.3	0.3	
	Dual-horizontal	63.9	2.9	59.8	2.6	
	Dual-vertical	64.6	2.9	62.6	2.6	
Visual task	Single	95.4	1.2	96.5	0.7	
	Dual-horizontal	76.0	2.9	78.8	2.7	
	Dual-vertical	72.1	3.0	75.3	2.5	

Table 2

Mean response times (in seconds) as a function of Culture, Presentation format,

Condition, and Problem complexity. Standard errors in parentheses.

		Canadian		Chinese		
Task	Load Type	Easy	Difficult	Easy	Difficult	
Subtraction	(Experiment 1)					
Horizontal	None	3.44 (0.3)	5.89 (0.5)	2.15 (0.1)	3.44 (0.1)	
	Phonological	4.01 (0.4)	5.97 (0.6)	2.52 (0.1)	3.85 (0.2)	
	Visual	3.69 (0.3)	6.20 (0.5)	2.48 (0.1)	3.91 (0.2)	
Vertical	None	2.93 (0.2)	5.22 (0.5)	1.94 (0.1)	3.18 (0.2)	
	Phonological	3.24 (0.4)	6.07 (0.6)	2.35 (0.1)	3.55 (0.3)	
	Visual	3.26 (0.3)	5.80 (0.5)	2.23 (0.1)	3.37 (0.2)	
Multiplication (Experiment 2)						
Horizontal	None	3.89 (0.3)	5.19 (0.5)	2.40 (0.1)	3.05 (0.2)	
	Phonological	4.40 (0.3)	6.09 (0.6)	2.77 (0.2)	3.34 (0.2)	
	Visual	4.60 (0.4)	5.88 (0.5)	2.73 (0.1)	3.48 (0.3)	
Vertical	None	3.66 (0.3)	4.84 (0.4)	2.22 (0.1)	2.66 (0.2)	
	Phonological	4.32 (0.3)	5.60 (0.5)	2.70 (0.2)	3.25 (0.2)	
	Visual	4.23 (0.3)	5.36 (0.4)	2.67 (0.2)	3.27 (0.2)	

Table 3

Error rates (%) as a function of Culture, Presentation format, Condition, and Problem complexity. Standard errors in parentheses.

		Canadian		Chinese		
Task	Load Type	Easy	Difficult	Easy	Difficult	
Subtraction (E	experiment 1)					
Horizontal	No load	7.46 (1.9)	18.31 (4.3)	5.03 (1.3)	11.82 (2.2)	
	Phonological	5.69 (1.6)	22.42 (3.7)	5.59 (1.2)	13.07 (2.1)	
	Visual	8.96 (2.3)	20.19 (4.4)	7.43 (1.5)	11.11 (2.1)	
Vertical	No load	4.69 (1.3)	19.54 (4.1)	5.59 (1.5)	13.70 (2.8)	
	Phonological	4.23 (1.3)	21.77 (3.9)	5.85 (1.2)	14.33 (2.0)	
	Visual	7.92 (2.9)	21.12 (4.5)	3.82 (1.0)	13.05 (2.6)	
Multiplication (Experiment 2)						
Horizontal	No load	10.08 (2.3)	17.30 (3.4)	5.20 (1.3)	9.56 (1.8)	
	Phonological	10.93 (1.7)	15.62 (2.4)	7.33 (1.4)	14.09 (2.1)	
	Visual	9.51 (2.2)	18.5 (3.2)	3.80 (0.8)	11.77 (1.9)	
Vertical	No load	7.78 (1.8)	18.45 (3.8)	4.81 (1.1)	6.95 (1.7)	
	Phonological	8.40 (1.6)	17.20 (4.2)	6.24 (1.4)	9.38 (1.5)	
	Visual	8.04 (1.7)	18.13 (3.5)	7.52 (1.2)	9.97 (2.0)	