

Open-source modern modeling software: the R package lavaan

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contents

- part I:
 - software for modern modeling methods
 - software for SEM
 - lavaan is for statisticians, teachers and applied users
 - lavaan features (and missing features)
 - lavaan model syntax
- part II:
 - lavaan functions and options
 - lavaan and the (computational) history of SEM
 - future plans
 - discussion/questions

software for modern modeling methods: two approaches

- closed-source software
 - often highly advanced features
 - standalone (not integrated in a larger statistical package)
 - black box:
no access to internal data, no access to internal functions
 - commercial (cost, licensing issues, no information about bugs)
- open-source software
 - in some areas, less advanced features
 - often integrated (R package, Stata module, Matlab toolbox)
 - open: full access to internal data, internal functions
 - flexibility: can be extended, modified or embedded in a larger pipeline
 - (academic) community

software for SEM: commercial – closed-source

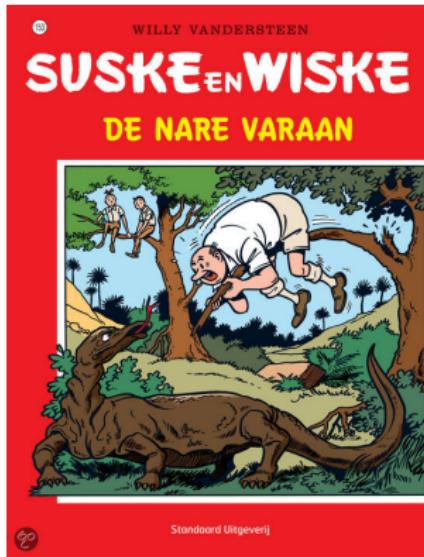
- the big four:
 - LISREL
 - EQS
 - AMOS
 - Mplus
- SAS/Stat: proc CALIS, proc TCALIS
- SEPATH (Statistica), RAMONA (Systat), Stata 12
- Mx (free, closed-source)

software for SEM: non-commercial – open-source

- outside the R ecosystem: gllamm (Stata module), ...
- R packages:
 - sem
 - OpenMx
 - lavaan
 - lava
- interfaces between R and commercial packages:
 - REQS
 - MplusAutomation

what is lavaan?

- **lavaan** is an R package for latent variable analysis



- the long-term goal of **lavaan** is to implement all the state-of-the-art capabilities that are currently available in commercial packages

installing lavaan, finding documentation

- **lavaan** depends on the R project for statistical computing:

<http://www.r-project.org>

- to install **lavaan**, simply start up an R session and type:

```
> install.packages("lavaan")
```

- more information about **lavaan**:

<http://lavaan.org>

- the **lavaan** paper:

Rosseel (2012). lavaan: an R package for structural equation modeling. *Journal of Statistical Software*, 48(2), 1–36.

- **lavaan** discussion group (mailing list)

<https://groups.google.com/d/forum/lavaan>

why do we need lavaan?

1. **lavaan** is for statisticians working in the field of SEM

- it seems unfortunate that new developments in this field are hindered by the lack of open source software that researchers can use to implement their newest ideas

2. **lavaan** is for teachers

- teaching these techniques to students was often complicated by the forced choice for one of the commercial packages

3. **lavaan** is for applied researchers

- keep it simple, provide all the features they need

lavaan is for statisticians working in the field of SEM (1)

- case-study: van de Schoot, R., Hoijtink, H. and Deković, M. (2010). Testing Inequality Constrained Hypotheses in SEM Models. *Structural Equation Modeling*, 17, 443-463

Testing Inequality Constrained Hypotheses in SEM Models

Rens van de Schoot and Herbert Hoijtink

*Department of Methods and Statistics
Utrecht University, The Netherlands*

Maja Deković

*Department of Child and Adolescent Studies
Utrecht University, The Netherlands*

Researchers often have expectations that can be expressed in the form of inequality constraints among the parameters of a structural equation model. It is currently not possible to test these so-called informative hypotheses in structural equation modeling software. We offer a solution to this problem using *Mplus*. The hypotheses are evaluated using plug-in *p* values with a calibrated alpha level. The method is introduced and its utility is illustrated by means of an example.

van de Schoot (1)

- the problem: testing *informative* hypotheses in a SEM model

$$H_0 : \beta_{\text{male}} = \beta_{\text{female}} \quad \text{versus} \quad H_c : \beta_{\text{male}} > \beta_{\text{female}} \quad (\text{Type A})$$

- van de Schoot et.al. (2010) present a frequentist solution: parametric bootstrap of the LRT to obtain a plug-in p-value
- seven steps:
 - estimate model under H_0 ($\beta_{\text{male}} = \beta_{\text{female}}$), save results
 - estimate model under H_c ($\beta_{\text{male}} > \beta_{\text{female}}$), save results
 - (manually) compute LRT.obs ($\log L_c - \log L_0$)
 - generate (R=1000) datasets under H_0
 - for each generated dataset, estimate H_0 and H_c model
 - (manually) compute (R=1000) LRT values,
 - compute plug-in p-value (proportion of LRTs \geq LRT.obs)

van de Schoot (2)

- but under the null, the plug-in p-values should be (asymptotically) uniformly distributed; unfortunately, in this setting, this is not the case
- van de Schoot et.al. (2010) use a ‘double bootstrap’ procedure to calibrate the alpha (α) level:
 - each ‘bootstrap sample’ is again ‘bootstrapped’ ($R=1000$)
 - we end up with R plug-in p-values, and the 5th percentile provides α^* (the calibrated alpha)
 - we should use α^* instead of the regular $\alpha = 0.05$
- challenge: try to do this using black box commercial SEM software ...
 - van de Schoot et.al. (2010) used Mplus, combined with a handful of custom R scripts (MplusAutomation was not available yet)

van de Schoot (3)

- what if we could do this in R?
- Leonard Vanbrabant wrote a high-level function to do all this in one simple step (available in **lavaan**)
- code snippet:

```
# simple regression model
model <- 'anti ~ b1*pos + b2*neg + b3*dis'

# inequality constraints (Hc)
constraints <- 'b1 < b3
                b2 < b3'

# compute plug-in p-value based on the double-bootstrap procedure
out <- InformativeTesting(model, data = social,
                           verbose = TRUE,
                           constraints = constraints,
                           R = 1000, type = "parametric",
                           double.bootstrap = "standard")
```

informative Testing output

Variable names in model : anti pos neg dis
Number of variables : 4
Number of groups : 1
Used sample size per group : 596
Used sample size : 596
Total sample size : 603

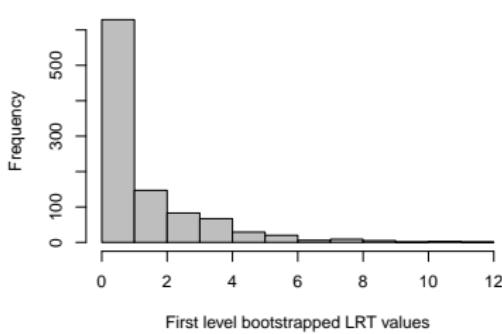
Estimator : ML
Missing data : listwise
Bootstrap method : parametric
Double bootstrap method : standard

Order Constrained Hypothesis Testing:

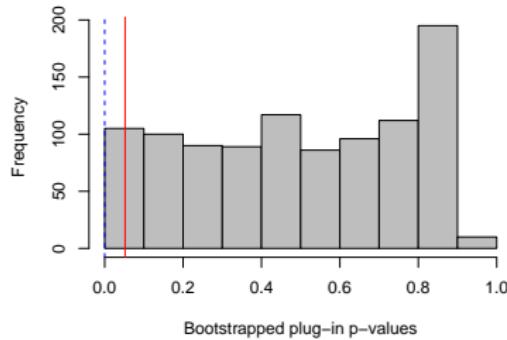
	Type A	Type B
LR statistic	47.98	00.05
P-value	0.00	0.43
Adjusted alpha	0.05	0.04
Adjusted p-value	0.00	0.79
Alpha	0.05	0.05
Significance	Significant	Non-significant

informativeTesting plot

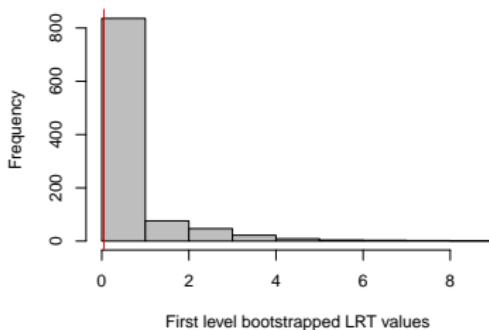
Distribution of bootstrapped LRT values – Type A



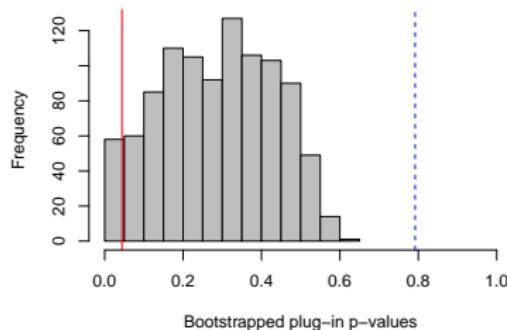
Distribution of plug-in p-values – Type A



Distribution of bootstrapped LRT values – Type B



Distribution of plug-in p-values – Type B



lavaan is for statisticians working in the field of SEM (2)

- case-study: Myrsini Katsikatsou (2012), Ph.D. dissertation, Paper 4

Pairwise likelihood estimation for structural
equation modeling with ordinal and continuous
variables

Myrsini Katsikatsou

Department of Statistics, Uppsala University, Sweden

Abstract

A pairwise likelihood (PL) estimation method is developed for structural equation models (SEM) with continuous and ordinal observed variables where covariates may also be included. The proposed methodology starts off with the development of PL for estimating the mean vector and the covariance matrix of a variable vector consisting of continuous and ordinal variables. Later on a parametric structure is given to the mean vector and the covariance matrix according to a general SEM. The suggested method is demonstrated using an example with empirical data. An R code has been written which has been implemented in the R package `lavaan` (version 0.5-11). Maximum likelihood estimation, as implemented in Mplus (version 5.21) and in LISREL (version 9.10), is not feasible for our example due to its high computational complexity.

- a lot of the infrastructure for the PML estimator is already present in commercial software (but inaccessible)

lavaan is for statisticians working in the field of SEM (3)

- case-study: Merkle, E.C. and Zeileis, A. (2013). Tests of measurement invariance without subgroups: a generalization of classical methods. *Psychometrika*, 78, 59–82

8. Computational Details

All results were obtained using the R system for statistical computing (R Development Core Team, 2012, version 2.15.0, employing the add-on packages lavaan 0.4-14 (Rosseel, 2012) and OpenMx 1.1.1-1785 (Boker, Neale, Maes, Wilde, Spiegel, Brick, & et al., 2011) for fitting of the factor analysis models and strucchange 1.4-7 (Zeileis, Leisch, Hornik, & Kleiber, 2002; Zeileis, 2006) for evaluating the parameter instability tests. R and the packages lavaan and strucchange are freely available under the General Public License 2 from the Comprehensive R Archive Network at <http://CRAN.R-project.org/> while OpenMx is available under the Apache License 2.0 from <http://OpenMx.psyc.virginia.edu/>. R code for replication of our results is available at <http://semtools.R-Forge.R-project.org/>.

- again, computations were needed (eg. case-wise scores) that are commonly computed by commercial packages (but we can not extract the results)

lavaan is for teachers

- case-study:
 - doctoral school SEM course in a Faculty of Psychology and Education Sciences; 40 Ph.D. students from 7 different departments; 5 departments had previously bought several licenses for either LISREL(2), EQS(1), AMOS(2)*
 - which software package should we choose?
 - what is the cost? (we prefer the full version)
- the lavaan syntax is easy to learn
- learning an R package will increase general R skills
- the ‘mimic’ option in lavaan makes a smooth transition possible from lavaan to one of the major commercial programs (and back)
- share your teaching materials:

<http://lavaan.ugent.be/resources/teaching.html/>

lavaan is for applied researchers

- what matters most to many applied researchers:
 - the software is easy and intuitive to use
 - the software has all the features they want
 - results of lavaan are very close, if not identical, to those reported by their current commercial program
- a 37-pages tutorial should get you started right away

`http://lavaan.ugent.be/tutorial/`

- you will be able to replicate your results (say, after ten years)

`http://lavaan.ugent.be/history/`

features of lavaan

- **lavaan** is well-tested
- user-friendly fitting functions (cfa, sem, growth)
- power-user fitting function (lavaan)
- support for non-normal continuous data:
 - robust standard errors, Satorra-Bentler correction, ADF estimation, bootstrapping
- support for categorical (binary/ordinal) data
 - **lavaan** has implemented the three-stage WLS approach as developed by Bengt Muthén (1984); including robust variants (aka WLSMV)
- full support for missing data (fiml), meanstructures, and multiple groups
- linear and non-linear equality and inequality constraints

unique features

- default model specification: lavaan model syntax
 - mplus2lavaan (Michael Hallquist, included in lavaan 0.5-13)
 - lisrel2lavaan (Corbin Quick, included in the semTools package)
 - graphical (via Onyx)
 - ...
- mimic the (numerical) results of commercial packages:
 - mimic="Mplus"
 - mimic="EQS"
- new technical features:
 - informative hypothesis testing (Leonard Vanbrabant)
 - pairwise ML for binary/ordinal data (Myrsini Katsikatsou)
 - fraction of missing information (Mijke Rhemtulla)
 - ...

features NOT in lavaan (yet)

- multilevel SEM
- mixture (latent class) SEM
- ...

features we are working on

- Bayesian SEM (BUGS interface, stan interface, native)
- small-sample corrections
- causal inference
- standard errors for standardized parameters
- ML estimation for categorical data (IRT)
- ...
- better (technical) documentation

the lavaan ecosystem

- **lavaan.survey** (Daniel Oberski)

survey weights, clustering, strata, and finite sampling corrections
in SEM (including support for replicate weights, eg. PISA)

- **Onyx** (Timo von Oertzen, Andreas M. Brandmaier, Siny Tsang)

interactive graphical interface for SEM (written in Java)

- **semTools** (Sunthud Pornprasertmanit and many others)

collection of useful functions for SEM

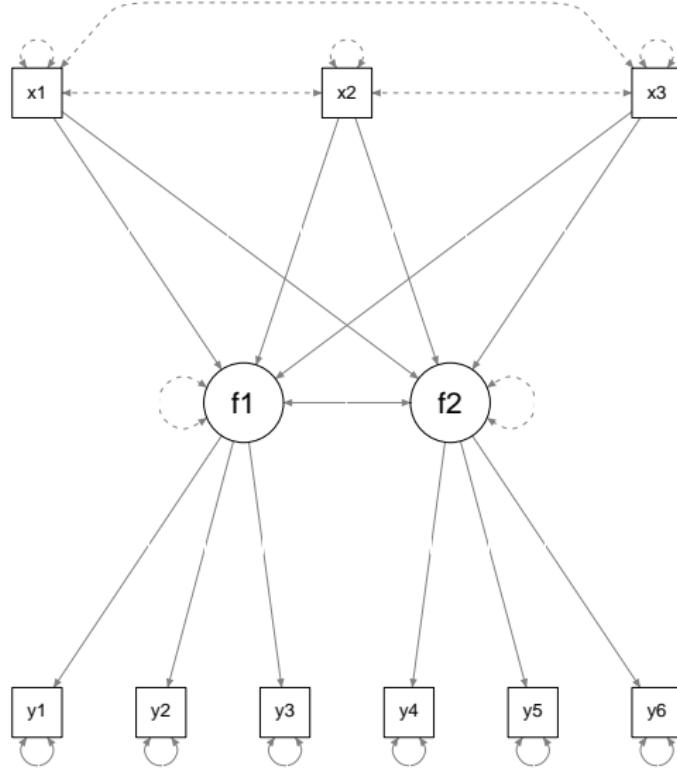
- **simsem** (Sunthud Pornprasertmanit and many others)

simulation of SEM models

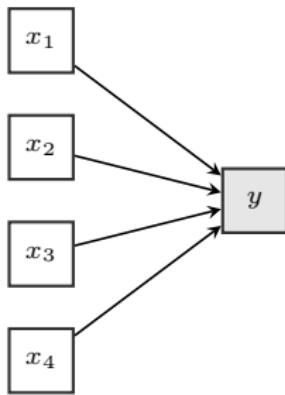
- **semPlot** (Sacha Epskamp)

visualizations of SEM models

semPlot



a simple regression analysis in R



```
# read in your data  
myData <- read.csv("c:/temp/myData.csv")  
  
# fit model using lm  
fit <- lm(formula = y ~ x1 + x2 + x3 + x4,  
          data    = myData)  
  
# show results  
summary(fit)
```

The standard linear model:

- $y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \beta_3 x_{i3} + \beta_4 x_{i4} + \epsilon_i \quad (i = 1, 2, \dots, n)$

lm() output artificial data (N=100)

Call:

```
lm(formula = y ~ x1 + x2 + x3 + x4, data = myData)
```

Residuals:

Min	1Q	Median	3Q	Max
-102.372	-29.458	-3.658	27.275	148.404

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	97.7210	4.7200	20.704	<2e-16 ***
x1	5.7733	0.5238	11.022	<2e-16 ***
x2	-1.3214	0.4917	-2.688	0.0085 **
x3	1.1350	0.4575	2.481	0.0149 *
x4	0.2707	0.4779	0.566	0.5724

Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1 1

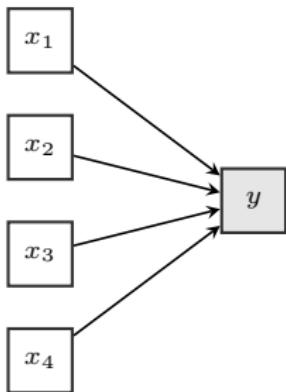
Residual standard error: 46.74 on 95 degrees of freedom

Multiple R-squared: 0.5911, Adjusted R-squared: 0.5738

F-statistic: 34.33 on 4 and 95 DF, p-value: < 2.2e-16

```
# create artificial data
set.seed(1)
x1 <- rnorm(100) * 10; x2 <- rnorm(100) * 10
x3 <- rnorm(100) * 10; x4 <- rnorm(100) * 10
y <- 100 + 5*x1 + (-2)*x2 + 1*x3 + 0.1*x4 + rnorm(100, sd=40)
myData <- data.frame(y,x1,x2,x3,x4)
```

the lavaan model syntax – a simple regression



```
library(lavaan)
myData <- read.csv("c:/temp/myData.csv")

myModel <- ' y ~ x1 + x2 + x3 + x4 '

# fit model
fit <- sem(model = myModel,
            data  = myData)

# show results
summary(fit)
```

- to ‘see’ the intercept, use either

```
fit <- sem(model=myModel, data=myData, meanstructure=TRUE)
```

or include it explicitly in the syntax:

```
myModel <- ' y ~ 1 + x1 + x2 + x3 + x4 '
```

output (artificial data, N=100)

lavaan (0.5-13) converged normally after 1 iterations

Number of observations 100

Estimator ML

Minimum Function Test Statistic 0.000

Degrees of freedom 0

P-value (Chi-square) 1.000

Parameter estimates:

Information	Expected
-------------	----------

Standard Errors	Standard
-----------------	----------

	Estimate	Std.error	Z-value	P(> z)
--	----------	-----------	---------	---------

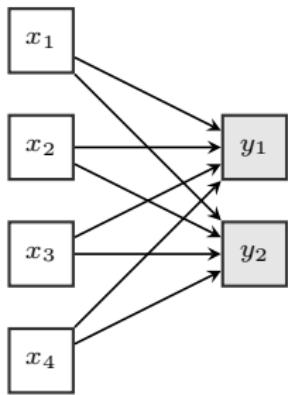
Regressions:

y ~	x1	5.773	0.511	11.309	0.000
	x2	-1.321	0.479	-2.757	0.006
	x3	1.135	0.446	2.545	0.011
	x4	0.271	0.466	0.581	0.561

Variances:

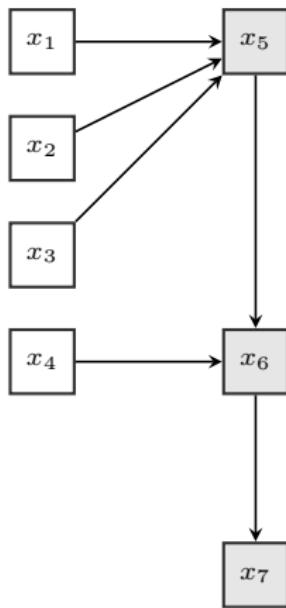
y	2075.100	293.463
---	----------	---------

the lavaan model syntax – multivariate regression



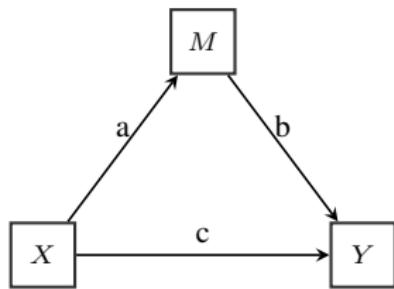
```
myModel <- ' y1 ~ x1 + x2 + x3 + x4  
          y2 ~ x1 + x2 + x3 + x4 '
```

the lavaan model syntax – path analysis



```
myModel <- ' x5 ~ x1 + x2 + x3  
x6 ~ x4 + x5  
x7 ~ x6 ',
```

the lavaan model syntax – mediation analysis



```
model <- '
  Y ~ b*M + c*X
  M ~ a*X

  indirect := a*b
  total    := c + (a*b)

  ,
  fit <- sem(model,
             data = myData,
             se = "bootstrap")
summary(fit)
```

output

...

Parameter estimates:

Information	Observed
Standard Errors	Bootstrap
Number of requested bootstrap draws	1000
Number of successful bootstrap draws	1000

	Estimate	Std.err	Z-value	P(> z)
--	----------	---------	---------	---------

Regressions:

Y ~					
M	(b)	0.597	0.098	6.068	0.000
X	(c)	2.594	1.210	2.145	0.032
M ~					
X	(a)	2.739	0.999	2.741	0.006

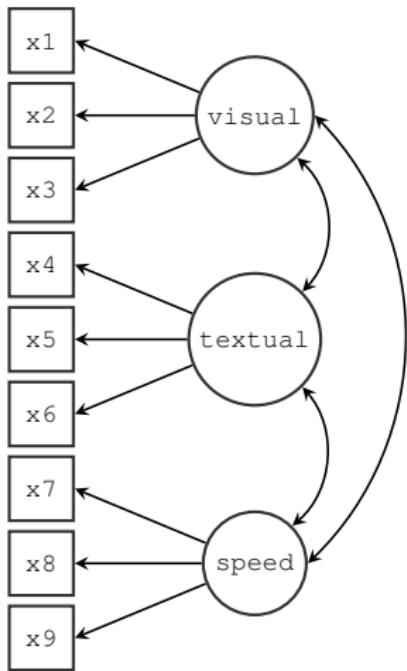
Variances:

Y	108.700	17.747
M	105.408	16.556

Defined parameters:

indirect	1.636	0.645	2.535	0.011
total	4.230	1.383	3.059	0.002

the lavaan model syntax – using cfa() or sem()



```
HS.model <- ' visual =~ x1 + x2 + x3  
            textual =~ x4 + x5 + x6  
            speed   =~ x7 + x8 + x9  
,  
  
fit <- cfa(model = HS.model,  
           data  = HolzingerSwineford1939)  
  
summary(fit, fit.measures = TRUE,  
        standardized = TRUE)
```

output

lavaan (0.5-13) converged normally after 35 iterations

Number of observations 301

Estimator ML

Minimum Function Test Statistic 85.306

Degrees of freedom 24

P-value (Chi-square) 0.000

Model test baseline model:

Minimum Function Test Statistic 918.852

Degrees of freedom 36

P-value 0.000

Full model versus baseline model:

Comparative Fit Index (CFI) 0.931

Tucker-Lewis Index (TLI) 0.896

Loglikelihood and Information Criteria:

Loglikelihood user model (H0) -3737.745

Loglikelihood unrestricted model (H1) -3695.092

Number of free parameters 21

Akaike (AIC)	7517.490
Bayesian (BIC)	7595.339
Sample-size adjusted Bayesian (BIC)	7528.739

Root Mean Square Error of Approximation:

RMSEA	0.092
90 Percent Confidence Interval	0.071 0.114
P-value RMSEA <= 0.05	0.001

Standardized Root Mean Square Residual:

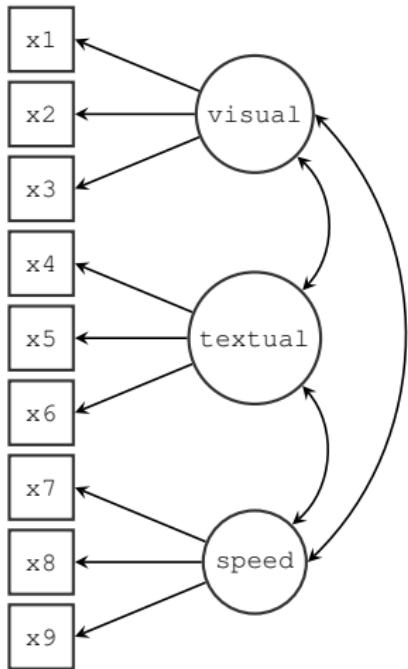
SRMR	0.065
------	-------

Parameter estimates:

	Information Standard Errors	Expected Standard				
		Estimate	Std.err	Z-value	P(> z)	Std.lv
Latent variables:						
visual =~						
x1	1.000				0.900	0.772
x2	0.554	0.100	5.554	0.000	0.498	0.424
x3	0.729	0.109	6.685	0.000	0.656	0.581
textual =~						
x4	1.000				0.990	0.852
x5	1.113	0.065	17.014	0.000	1.102	0.855

x6	0.926	0.055	16.703	0.000	0.917	0.838
speed =~						
x7	1.000				0.619	0.570
x8	1.180	0.165	7.152	0.000	0.731	0.723
x9	1.082	0.151	7.155	0.000	0.670	0.665
Covariances:						
visual ~~						
textual	0.408	0.074	5.552	0.000	0.459	0.459
speed	0.262	0.056	4.660	0.000	0.471	0.471
textual ~~						
speed	0.173	0.049	3.518	0.000	0.283	0.283
Variances:						
x1	0.549	0.114			0.549	0.404
x2	1.134	0.102			1.134	0.821
x3	0.844	0.091			0.844	0.662
x4	0.371	0.048			0.371	0.275
x5	0.446	0.058			0.446	0.269
x6	0.356	0.043			0.356	0.298
x7	0.799	0.081			0.799	0.676
x8	0.488	0.074			0.488	0.477
x9	0.566	0.071			0.566	0.558
visual	0.809	0.145			1.000	1.000
textual	0.979	0.112			1.000	1.000
speed	0.384	0.086			1.000	1.000

the lavaan model syntax – using lavaan()



```
HS.model <- '
  # latent variables
  visual   =~ 1*x1 + x2 + x3
  textual  =~ 1*x4 + x5 + x6
  speed    =~ 1*x7 + x8 + x9

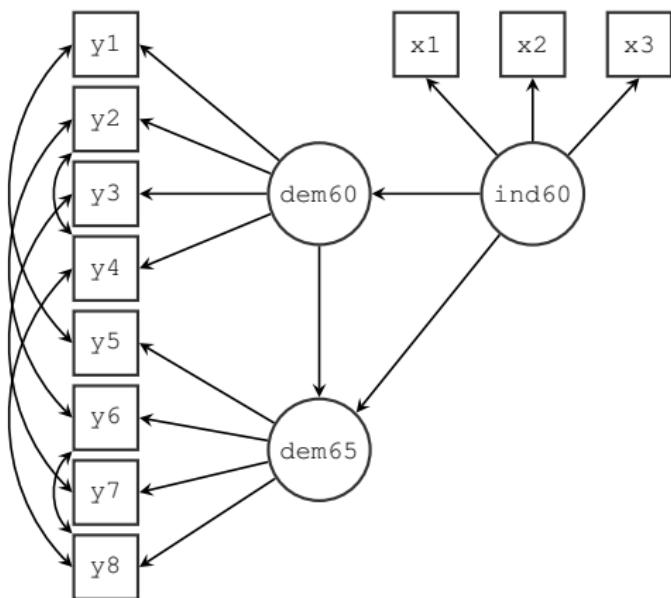
  # factor (co)variances
  visual ~~ visual; visual ~~ textual
  visual ~~ speed; textual ~~ textual
  textual ~~ speed; speed ~~ speed

  # residual variances
  x1 ~~ x1; x2 ~~ x2; x3 ~~ x3
  x4 ~~ x4; x5 ~~ x5; x6 ~~ x6
  x7 ~~ x7; x8 ~~ x8; x9 ~~ x9

  ,

  fit <- lavaan(model = HS.model,
                 data = HolzingerSwineford1939)
```

lavaan model syntax: full sem



```

myModel <- '

# latent variable definitions
ind60 =~ x1 + x2 + x3
dem60 =~ y1 + a*y2 + b*y3 + c*y4
dem65 =~ y5 + a*y6 + b*y7 + c*y8

# regressions
dem60 ~ ind60
dem65 ~ ind60 + dem60

# residual covariances
y1 ~~ y5
y2 ~~ y4
y2 ~~ y6
y3 ~~ y7
y4 ~~ y8
y6 ~~ y8

'

fit <- sem(model = myModel,
           data = ...)

```

output

lavaan (0.5-13) converged normally after 61 iterations

Number of observations 75

Estimator	ML
Minimum Function Test Statistic	40.179
Degrees of freedom	38
P-value (Chi-square)	0.374

Parameter estimates:

	Information	Standard Errors	Expected	Standard
	Estimate	Std.err	Z-value	P(> z)
Latent variables:				
ind60 =~				
x1	1.000			
x2	2.180	0.138	15.751	0.000
x3	1.818	0.152	11.971	0.000
dem60 =~				
y1	1.000			
y2 (a)	1.191	0.139	8.551	0.000
y3 (b)	1.175	0.120	9.755	0.000
y4 (c)	1.251	0.117	10.712	0.000
dem65 =~				

y5		1.000			
y6	(a)	1.191	0.139	8.551	0.000
y7	(b)	1.175	0.120	9.755	0.000
y8	(c)	1.251	0.117	10.712	0.000

Regressions:

dem60	~				
ind60		1.471	0.392	3.750	0.000
dem65	~				
ind60		0.600	0.226	2.660	0.008
dem60		0.865	0.075	11.554	0.000

Covariances:

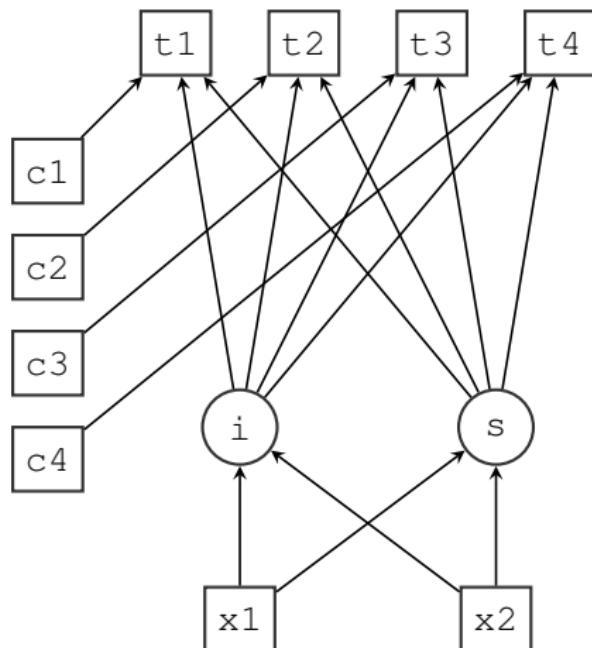
y1	~~				
y5		0.583	0.356	1.637	0.102
y2	~~				
y4		1.440	0.689	2.092	0.036
y6		2.183	0.737	2.960	0.003
y3	~~				
y7		0.712	0.611	1.165	0.244
y4	~~				
y8		0.363	0.444	0.817	0.414
y6	~~				
y8		1.372	0.577	2.378	0.017

Variances:

x1		0.081	0.019		
x2		0.120	0.070		

x3	0.467	0.090
y1	1.855	0.433
y2	7.581	1.366
y3	4.956	0.956
y4	3.225	0.723
y5	2.313	0.479
y6	4.968	0.921
y7	3.560	0.710
y8	3.308	0.704
ind60	0.449	0.087
dem60	3.875	0.866
dem65	0.164	0.227

a simple growth curve model with time-varying covariates



```
model <- '
  # random intercept and slope
  i =~ 1*t1 + 1*t2 + 1*t3 + 1*t4
  s =~ 0*t1 + 1*t2 + 2*t3 + 3*t4

  # regressions
  i ~ x1 + x2
  s ~ x1 + x2

  # time-varying covariates
  t1 ~ c1
  t2 ~ c2
  t3 ~ c3
  t4 ~ c4
  ,

fit <- growth(model, data=Demo.growth)
summary(fit)
```

further syntax

- fixing parameters, and overriding auto-fixed parameters

```
HS.model.bis <- ' visual  =~ NA*x1 + x2 + x3  
                  textual =~ NA*x4 + x5 + x6  
                  speed   =~ NA*x7 + x8 + x9  
                  visual  ~~ 1*visual  
                  textual ~~ 1{textual}  
                  speed   ~~ 1*speed  
,
```

- linear and nonlinear equality and inequality constraints

```
model.constr <- ' # model with labeled parameters  
                  y ~ b1*x1 + b2*x2 + b3*x3  
  
                  # constraints  
                  b1 == (b2 + b3)^2  
                  b1 > exp(b2 + b3) '
```

- several modifiers (eg. fix and label)

```
myModel <- ' y ~ 0.5*x1 + x2 + x3 + b1*x1 '
```

user-friendly fitting functions

- `cfa()` for confirmatory factor analysis
- `sem()` for path analysis and SEM
- `growth()` for growth curve modeling

arguments of the `cfa()` and `sem()` fitting functions

```
sem(model = NULL, meanstructure = "default", fixed.x = "default",
     orthogonal = FALSE, std.lv = FALSE, data = NULL, std.ov = FALSE,
     missing = "default", sample.cov = NULL, sample.mean = NULL,
     sample.nobs = NULL, group = NULL, group.equal = "",
     group.partial = "", constraints = '', estimator = "default",
     likelihood = "default", information = "default", se = "default",
     test = "default", bootstrap = 1000L,
     mimic = "default", representation = "default",
     do.fit = TRUE, control = list(), start = "default",
     verbose = FALSE, warn = TRUE, debug = FALSE)
```

power-user fitting functions

- `lavaan()` by default, no model parameters are added automagically to the parameter table
- several `auto.*` arguments are available to
 - automatically add a set of parameters (e.g. all (residual) variances)
 - take actions to make the model identifiable (e.g. set the metric of the latent variables)

example using lavaan with an `auto.*` argument

```
HS.model.mixed <- ' # latent variables
                    visual   =~ 1*x1 + x2 + x3
                    textual  =~ 1*x4 + x5 + x6
                    speed    =~ 1*x7 + x8 + x9
                    # factor covariances
                    visual   ~~ textual + speed
                    textual  ~~ speed

,
fit <- lavaan(HS.model.mixed, data=HolzingerSwineford1939,
               auto.var=TRUE)
```

auto.* flags

keyword	operator	parameter set
auto.var	~ ~	(residual) variances observed and latent variables
auto.cov.y	~ ~	(residual) covariances observed and latent endogenous variables
auto.cov.lv.x	~ ~	covariances among exogenous latent variables
keyword	default	action
auto.fix.first	TRUE	fix the factor loading of the first indicator to 1
auto.fix.single	TRUE	fix the residual variance of a single indicator to 1
int.ov.free	TRUE	freely estimate the intercepts of the observed variables (only if a mean structure is included)
int.lv.free	FALSE	freely estimate the intercepts of the latent variables (only if a mean structure is included)

extractor functions: inspecting fitted models

Method	Description
summary ()	print a long summary of the model results
show ()	print a short summary of the model results
coef ()	returns the estimates of the free parameters in the model as a named numeric vector
fitted ()	returns the implied moments (covariance matrix and mean vector) of the model
resid ()	returns the raw, normalized or standardized residuals (difference between implied and observed moments)
vcov ()	returns the covariance matrix of the estimated parameters
predict ()	compute factor scores
logLik ()	returns the log-likelihood of the fitted model (if maximum likelihood estimation was used)
AIC (), BIC ()	compute information criteria (if maximum likelihood estimation was used)
update ()	update a fitted lavaan object
inspect ()	peek into the internal representation of the model; by default, it returns a list of model matrices counting the free parameters in the model; can also be used to extract starting values, gradient values, and much more

other functions

Function	Description
<code>lavaanify()</code>	converts a lavaan model syntax to a parameter table
<code>parameterTable()</code>	returns the parameter table
<code>parameterEstimates()</code>	returns the parameter estimates, including confidence intervals, as a data frame
<code>standardizedSolution()</code>	returns one of three types of standardized parameter estimates, as a data frame
<code>modindices()</code>	computes modification indices and expected parameter changes
<code>bootstrapLavaan()</code>	bootstrap any arbitrary statistic that can be extracted from a fitted lavaan object
<code>bootstrapLRT()</code>	bootstrap a chi-square difference test for comparing to alternative models

extractor examples (1)

```
> fit <- cfa(HS.model, data=HolzingerSwineford1939)
> fitted(fit)
$cov
   x1    x2    x3    x4    x5    x6    x7    x8    x9
x1 1.358
x2 0.448 1.382
x3 0.590 0.327 1.275
x4 0.408 0.226 0.298 1.351
x5 0.454 0.252 0.331 1.090 1.660
x6 0.378 0.209 0.276 0.907 1.010 1.196
x7 0.262 0.145 0.191 0.173 0.193 0.161 1.183
x8 0.309 0.171 0.226 0.205 0.228 0.190 0.453 1.022
x9 0.284 0.157 0.207 0.188 0.209 0.174 0.415 0.490 1.015

$mean
x1 x2 x3 x4 x5 x6 x7 x8 x9
 0  0  0  0  0  0  0  0  0

> predict(fit)
      visual textul speed
[1,] -0.818 -0.138  0.062
[2,]  0.050 -1.013  0.625
[3,] -0.761 -1.872 -0.841
[4,]  0.419  0.018 -0.271
[5,] -0.416 -0.122  0.194
...
```

extractor examples (2)

```
> inspect(fit) # matrix representation
$lambda
  visual textul speed
x1      0      0      0
x2      1      0      0
x3      2      0      0
x4      0      0      0
x5      0      3      0
x6      0      4      0
x7      0      0      0
x8      0      0      5
x9      0      0      6

$theta
  x1 x2 x3 x4 x5 x6 x7 x8 x9
x1  7
x2  0  8
x3  0  0  9
x4  0  0  0 10
x5  0  0  0  0 11
x6  0  0  0  0  0 12
x7  0  0  0  0  0  0 13
x8  0  0  0  0  0  0  0 14
x9  0  0  0  0  0  0  0  0 15

$psi
```

```
      visual textual speed
visual  16
textual 19     17
speed   20     21     18

> inspect(fit, "sampstat")
$cov
    x1     x2     x3     x4     x5     x6     x7     x8     x9
x1  1.358
x2  0.407  1.382
x3  0.580  0.451  1.275
x4  0.505  0.209  0.208  1.351
x5  0.441  0.211  0.112  1.098  1.660
x6  0.455  0.248  0.244  0.896  1.015  1.196
x7  0.085 -0.097  0.088  0.220  0.143  0.144  1.183
x8  0.264  0.110  0.212  0.126  0.181  0.165  0.535  1.022
x9  0.458  0.244  0.374  0.243  0.295  0.236  0.373  0.457  1.015

$mean
    x1     x2     x3     x4     x5     x6     x7     x8     x9
4.936 6.088 2.250 3.061 4.341 2.186 4.186 5.527 5.374
```

fitMeasures

```
> fitMeasures(fit)
      fmin          chisq           df       pvalue
      0.142        85.306        24.000      0.000
baseline.chisq baseline.df baseline.pvalue
      918.852      36.000        0.000      0.931
      tli          nnfi          rfi       nfi
      0.896        0.896        0.861      0.907
      pnfi          ifi          rni       logl
      0.605        0.931        0.931    -3737.745
unrestricted.logl      npar          aic       bic
      -3695.092     21.000      7517.490    7595.339
      ntotal         bic2        rmsea   rmsea.ci.lower
      301.000      7528.739      0.092      0.071
rmsea.ci.upper      rmsea.pvalue      rmr      rmr_nomean
      0.114        0.001        0.082      0.082
      srmr        srmr_nomean      cn_05      cn_01
      0.065        0.065      129.490     152.654
      gfi          agfi        pgfi       mfi
      0.943        0.894        0.503      0.903
      ecvi
      0.423
```

parameterTable

```
> parameterTable(fit)
   id    lhs op      rhs user group free ustart exo label eq.id unco
 1  1 visual =~    x1    1     1   0     1   0          0     0
 2  2 visual =~    x2    1     1   1    NA   0          0     1
 3  3 visual =~    x3    1     1   2    NA   0          0     2
 4  4 textual =~   x4    1     1   0     1   0          0     0
 5  5 textual =~   x5    1     1   3    NA   0          0     3
 6  6 textual =~   x6    1     1   4    NA   0          0     4
 7  7 speed  =~   x7    1     1   0     1   0          0     0
 8  8 speed  =~   x8    1     1   5    NA   0          0     5
 9  9 speed  =~   x9    1     1   6    NA   0          0     6
10 10      x1 ~~   x1    0     1   7    NA   0          0     7
11 11      x2 ~~   x2    0     1   8    NA   0          0     8
12 12      x3 ~~   x3    0     1   9    NA   0          0     9
13 13      x4 ~~   x4    0     1  10   NA   0          0    10
14 14      x5 ~~   x5    0     1  11   NA   0          0    11
15 15      x6 ~~   x6    0     1  12   NA   0          0    12
16 16      x7 ~~   x7    0     1  13   NA   0          0    13
17 17      x8 ~~   x8    0     1  14   NA   0          0    14
18 18      x9 ~~   x9    0     1  15   NA   0          0    15
19 19 visual ~~ visual 0     1  16   NA   0          0    16
20 20 textual ~~ textual 0     1  17   NA   0          0    17
21 21 speed  ~~ speed  0     1  18   NA   0          0    18
22 22 visual ~~ textual 0     1  19   NA   0          0    19
23 23 visual ~~ speed  0     1  20   NA   0          0    20
24 24 textual ~~ speed  0     1  21   NA   0          0    21
```

parameterEstimates

```
> parameterEstimates(fit)
   lhs op    rhs   est     se      z pvalue ci.lower ci.upper
1  visual =~      x1 1.000 0.000     NA     NA  1.000  1.000
2  visual =~      x2 0.554 0.100  5.554     0  0.358  0.749
3  visual =~      x3 0.729 0.109  6.685     0  0.516  0.943
4 textual =~      x4 1.000 0.000     NA     NA  1.000  1.000
5 textual =~      x5 1.113 0.065 17.014     0  0.985  1.241
6 textual =~      x6 0.926 0.055 16.703     0  0.817  1.035
7   speed =~      x7 1.000 0.000     NA     NA  1.000  1.000
8   speed =~      x8 1.180 0.165  7.152     0  0.857  1.503
9   speed =~      x9 1.082 0.151  7.155     0  0.785  1.378
10    x1 ~~      x1 0.549 0.114  4.833     0  0.326  0.772
11    x2 ~~      x2 1.134 0.102 11.146     0  0.934  1.333
12    x3 ~~      x3 0.844 0.091  9.317     0  0.667  1.022
13    x4 ~~      x4 0.371 0.048  7.779     0  0.278  0.465
14    x5 ~~      x5 0.446 0.058  7.642     0  0.332  0.561
15    x6 ~~      x6 0.356 0.043  8.277     0  0.272  0.441
16    x7 ~~      x7 0.799 0.081  9.823     0  0.640  0.959
17    x8 ~~      x8 0.488 0.074  6.573     0  0.342  0.633
18    x9 ~~      x9 0.566 0.071  8.003     0  0.427  0.705
19 visual ~~  visual 0.809 0.145  5.564     0  0.524  1.094
20 textual ~~ textual 0.979 0.112  8.737     0  0.760  1.199
21   speed ~~    speed 0.384 0.086  4.451     0  0.215  0.553
22 visual ~~ textual 0.408 0.074  5.552     0  0.264  0.552
23 visual ~~    speed 0.262 0.056  4.660     0  0.152  0.373
24 textual ~~    speed 0.173 0.049  3.518     0  0.077  0.270
```

varTable

```
> varTable(fit)
   name idx nobs    type exo user   mean   var nlev lnam
 1  x1   7 301 numeric  0    0 4.936 1.363    0
 2  x2   8 301 numeric  0    0 6.088 1.386    0
 3  x3   9 301 numeric  0    0 2.250 1.279    0
 4  x4  10 301 numeric  0    0 3.061 1.355    0
 5  x5  11 301 numeric  0    0 4.341 1.665    0
 6  x6  12 301 numeric  0    0 2.186 1.200    0
 7  x7  13 301 numeric  0    0 4.186 1.187    0
 8  x8  14 301 numeric  0    0 5.527 1.025    0
 9  x9  15 301 numeric  0    0 5.374 1.018    0
```

modification indices

```
> subset(modindices(fit), mi > 5)
   lhs op rhs    mi    epc sepc.lv sepc.all sepc.nox
1  visual =~ x5 7.441 -0.210  -0.189  -0.147  -0.147
2  visual =~ x7 18.631 -0.422  -0.380  -0.349  -0.349
3  visual =~ x9 36.411  0.577   0.519   0.515   0.515
4 textual =~ x1 8.903  0.350   0.347   0.297   0.297
5 textual =~ x3 9.151 -0.272  -0.269  -0.238  -0.238
6      x1 ~~ x7 5.420 -0.129  -0.129  -0.102  -0.102
7      x1 ~~ x9 7.335  0.138   0.138   0.117   0.117
8      x2 ~~ x3 8.532  0.218   0.218   0.164   0.164
9      x2 ~~ x7 8.918 -0.183  -0.183  -0.143  -0.143
10     x3 ~~ x5 7.858 -0.130  -0.130  -0.089  -0.089
11     x4 ~~ x6 6.220 -0.235  -0.235  -0.185  -0.185
12     x4 ~~ x7 5.920  0.098   0.098   0.078   0.078
13     x7 ~~ x8 34.145  0.536   0.536   0.488   0.488
14     x7 ~~ x9 5.183 -0.187  -0.187  -0.170  -0.170
15     x8 ~~ x9 14.946 -0.423  -0.423  -0.415  -0.415
```

bootstrapLavaan

```
fit <- cfa(HS.model, data=HolzingerSwineford1939, se="none")  
  
# get the test statistic for the original sample  
  
T.orig <- fitMeasures(fit, "chisq")  
  
# bootstrap to get bootstrap test statistics  
# we only generate 10 bootstrap sample in this example; in practice  
# you may wish to use a much higher number  
  
T.boot <- bootstrapLavaan(fit,  
                           R = 10,  
                           type = "bollen.stine",  
                           FUN = fitMeasures,  
                           fit.measures = "chisq")  
  
# compute a bootstrap based p-value  
  
pvalue.boot <- length(which(T.boot > T.orig))/length(T.boot)
```

testing for measurement invariance

```
# model 1: configural invariance  
fit1 <- cfa(HS.model, data=HolzingerSwineford1939, group="school")  
  
# model 2: weak invariance  
fit2 <- cfa(HS.model, data=HolzingerSwineford1939, group="school",  
            group.equal="loadings")  
  
# model 3: strong invariance  
fit3 <- cfa(HS.model, data=HolzingerSwineford1939, group="school",  
            group.equal=c("loadings", "intercepts"))
```

comparing two (nested) models: the anova() function

```
anova(fit1, fit2)
```

Chi Square Difference Test

Df	AIC	BIC	Chisq	Chisq diff	Df diff	Pr(>Chisq)
fit1	48	7484.4	7706.8	115.85		
fit2	54	7480.6	7680.8	124.04	6	0.2244

- this also works correctly if the chi-square test statistics are scaled (robust)

measurement invariance tests – all together

```
> library(semTools)
> measurementInvariance(HS.model, data=HolzingerSwineford1939,
  group="school", strict=FALSE)
```

Measurement invariance tests:

Model 1: configural invariance:

chisq	df	pvalue	cfi	rmsea	bic
115.851	48.000	0.000	0.923	0.097	7706.822

Model 2: weak invariance (equal loadings):

chisq	df	pvalue	cfi	rmsea	bic
124.044	54.000	0.000	0.921	0.093	7680.771

[Model 1 versus model 2]

delta.chisq	delta.df	delta.p.value	delta.cfi
8.192	6.000	0.224	0.002

Model 3: strong invariance (equal loadings + intercepts):

chisq	df	pvalue	cfi	rmsea	bic
164.103	60.000	0.000	0.882	0.107	7686.588

[Model 1 versus model 3]

delta.chisq	delta.df	delta.p.value	delta.cfi
48.251	12.000	0.000	0.041

[Model 2 versus model 3]

delta.chisq	delta.df	delta.p.value	delta.cfi
40.059	6.000	0.000	0.038

Model 4: equal loadings + intercepts + means:

chisq	df	pvalue	cfi	rmsea	bic
204.605	63.000	0.000	0.840	0.122	7709.969

[Model 1 versus model 4]

delta.chisq	delta.df	delta.p.value	delta.cfi
88.754	15.000	0.000	0.083

[Model 3 versus model 4]

delta.chisq	delta.df	delta.p.value	delta.cfi
40.502	3.000	0.000	0.042

missing data: fiml

```
fit <- cfa(HS.model,
            data = HolzingerSwineford1939,
            missing = "ml")
```

alternative estimators

```
fit <- cfa(HS.model,
            data = HolzingerSwineford1939,
            estimator = "GLS")
```

robust standard errors

```
fit <- cfa(HS.model,
            data = HolzingerSwineford1939,
            se = "robust")
```

Satorra-Bentler scaled test statistic

```
fit <- cfa(HS.model,
            data = HolzingerSwineford1939,
            test = "Satorra-Bentler")
```

shortcut: robust standard errors and scaled test statistic

```
> fit <- cfa(HS.model,
  data = HolzingerSwineford1939,
  estimator = "MLM")
> summary(fit, fit.measures=TRUE)
lavaan (0.5-13) converged normally after 35 iterations
```

Number of observations	301	
Estimator	ML	Robust
Minimum Function Test Statistic	85.306	80.872
Degrees of freedom	24	24
P-value (Chi-square)	0.000	0.000
Scaling correction factor for the Satorra-Bentler correction		1.055

Model test baseline model:

Minimum Function Test Statistic	918.852	789.298
Degrees of freedom	36	36
P-value	0.000	0.000

Full model versus baseline model:

Comparative Fit Index (CFI)	0.931	0.925
Tucker-Lewis Index (TLI)	0.896	0.887

...

mimic option

```
> cfa(HS.model, data = HolzingerSwineford1939,
      estimator = "MLM", mimetic = "EQS")
...
Estimator                               ML      Robust
Minimum Function Test Statistic        85.022   81.141
...
> cfa(HS.model, data = HolzingerSwineford1939,
      estimator = "MLM", mimetic = "Mplus")
...
Estimator                               ML      Robust
Minimum Function Test Statistic        85.306   81.908
...
> cfa(HS.model, data = HolzingerSwineford1939,
      estimator = "MLM", mimetic = "lavaan")
...
Estimator                               ML      Robust
Minimum Function Test Statistic        85.306   80.872
...
```

binary and ordered categorical data

```
# binary version of Holzinger & Swineford
HS9 <- HolzingerSwineford1939[,c("x1","x2","x3","x4","x5",
                                "x6","x7","x8","x9")]
HSbinary <- as.data.frame( lapply(HS9, cut, 2, labels=FALSE) )

# single factor model
model <- ' visual   =~ x1 + x2 + x3
            textual  =~ x4 + x5 + x6
            speed    =~ x7 + x8 + x9 '

# binary CFA
fit <- cfa(model, data=HSbinary, ordered=names(HSbinary))

# summary
summary(fit, fit.measures=TRUE)
```

output

lavaan (0.5-13) converged normally after 36 iterations

Number of observations

301

Estimator

DWLS

Robust

Minimum Function Test Statistic

30.918

38.546

Degrees of freedom

24

24

P-value (Chi-square)

0.156

0.030

Scaling correction factor

0.866

Shift parameter

2.861

for simple second-order correction (Mplus variant)

Model test baseline model:

Minimum Function Test Statistic

582.533

469.769

Degrees of freedom

36

36

P-value

0.000

0.000

Full model versus baseline model:

Comparative Fit Index (CFI)

0.987

0.966

Tucker-Lewis Index (TLI)

0.981

0.950

Root Mean Square Error of Approximation:

RMSEA

0.031

0.045

90 Percent Confidence Interval	0.000	0.059	0.014	0.070
P-value RMSEA <= 0.05		0.848		0.598

Parameter estimates:

	Information Standard Errors	Expected Robust.sem				
		Estimate	Std.err	Z-value	P(> z)	
Latent variables:						
visual =						
x1	1.000					
x2	0.900	0.188	4.788	0.000		
x3	0.939	0.197	4.766	0.000		
textual =						
x4	1.000					
x5	0.976	0.118	8.241	0.000		
x6	1.078	0.125	8.601	0.000		
speed =						
x7	1.000					
x8	1.569	0.461	3.403	0.001		
x9	1.449	0.409	3.541	0.000		
Covariances:						
visual ~~						
textual	0.303	0.061	4.981	0.000		
speed ~~	0.132	0.049	2.700	0.007		
textual ~~						

speed	0.076	0.046	1.656	0.098
Intercepts:				
visual	0.000			
textual	0.000			
speed	0.000			
Thresholds:				
x1 t1	-0.388	0.074	-5.223	0.000
x2 t1	-0.054	0.072	-0.748	0.454
x3 t1	0.318	0.074	4.309	0.000
x4 t1	0.180	0.073	2.473	0.013
x5 t1	-0.257	0.073	-3.506	0.000
x6 t1	1.024	0.088	11.641	0.000
x7 t1	0.231	0.073	3.162	0.002
x8 t1	1.128	0.092	12.284	0.000
x9 t1	0.626	0.078	8.047	0.000
Variances:				
x1	0.592			
x2	0.670			
x3	0.640			
x4	0.303			
x5	0.336			
x6	0.191			
x7	0.778			
x8	0.453			
x9	0.534			

visual	0.408	0.112
textual	0.697	0.101
speed	0.222	0.094

```
> inspect(fit, "sampstat")
$cov
  x1      x2      x3      x4      x5      x6      x7      x8      x9
x1 1.000
x2 0.284  1.000
x3 0.415  0.389  1.000
x4 0.364  0.328  0.232  1.000
x5 0.319  0.268  0.138  0.688  1.000
x6 0.422  0.322  0.206  0.720  0.761  1.000
x7 -0.048  0.061  0.041  0.200  0.023 -0.029  1.000
x8 0.159  0.105  0.439 -0.029 -0.059  0.183  0.464  1.000
x9 0.165  0.210  0.258  0.146  0.183  0.230  0.335  0.403  1.000

$mean
x1 x2 x3 x4 x5 x6 x7 x8 x9
 0  0  0  0  0  0  0  0  0

$th
 x1|t1  x2|t1  x3|t1  x4|t1  x5|t1  x6|t1  x7|t1  x8|t1  x9|t1
-0.388 -0.054  0.318  0.180 -0.257  1.024  0.231  1.128  0.626
```

the history of SEM, from a computational point of view

- several traditions in the SEM (software) world:
 - LISREL (Karl Jöreskog)
 - EQS (Peter Bentler)
 - Mplus (Bengt Muthén)
 - RAM-based approaches (AMOS, Mx, sem, OpenMx, ...)
- superficially, all SEM software packages produce the same results
- there are some subtle (and less subtle) differences in the output
- looking deeper, there are many computational differences

some differences

- matrix representation
 - standard number of matrices: LISREL: 8; Mplus: 4, EQS: 3, RAM: 2
- optimization algorithm
 - quasi-Newton, gradient-only + quasi-Newton, Gauss-Newton, ...
- variances constrained (strictly positive) versus unrestricted
- constrained optimization algorithm
 - mostly undocumented
 - a Lagrangian-multiplier variant, simple slacks, ...
- normal likelihood versus Wishart likelihood, ML versus RLS
 - N versus $N - 1$
 - GLS-ML based chi-square test statistic influences fit measures (CFI!)

some differences (2)

- Satorra-Bentler/Yuan-Bentler scaled test statistic
 - each program seems to use a different implementation
 - often asymptotically equivalent; but large differences in small samples
- categorical data using the limited information approach
 - Muthén 1984; Jöreskog 1994; Lee, Poon, Bentler (1992)
 - many ways to compute the asymptotic covariance matrix (needed for WLS)
- naive bootstrapping, Bollen-Stine bootstrapping
 - mostly undocumented; one-iteration bootstrap?
 - Bollen-Stine with missing data

...

lavaan and the history of SEM

- lavaan tries to preserve the many differences from the several traditions
- all fitting functions in lavaan have a `mimic` argument:
 - `mimic="EQS"`, `mimic="Mplus"`
 - `mimic="LISREL"` is under development
 - this was originally intended to convince users that lavaan could produce ‘identical’ results as the (commercial) competition
 - it is now one of the main design goals of lavaan
 - for reproducibility, we plan to make ‘mimic’ version-specific:
`mimic="Mplus4"`, `mimic="LISREL8"`, ...
- we need to (re)evaluate old/new/unexplored computational methods in many areas (optimization, constrained inference, Bayesian techniques, limited information estimation, ...)

version differences: Mplus 6/7 versus Mplus <6 (HSbinary example)

Mplus VERSION 7 (Linux)

...

MODEL FIT INFORMATION

Number of Free Parameters	21
---------------------------	----

Chi-Square Test of Model Fit

Value	38.546*
Degrees of Freedom	24
P-Value	0.0305

...

Mplus VERSION 4.1

...

TESTS OF MODEL FIT

Chi-Square Test of Model Fit

Value	32.074*
Degrees of Freedom	19**
P-Value	0.0307

...

Satterthwaite versus simple second-order correction

```
> cfa(model, data=HSbinary, ordered=names(HSbinary), mimic="Mplus")  
  
...  
Estimator DWLS Robust  
Minimum Function Test Statistic 30.918 38.546  
Degrees of freedom 24 24  
P-value (Chi-square) 0.156 0.030  
Scaling correction factor 0.866  
Shift parameter 2.861  
for simple second-order correction (WLSMV)  
  
> cfa(model, data=HSbinary, ordered=names(HSbinary), mimic="Mplus",  
estimator="WLSMVS")  
  
...  
Estimator DWLS Robust  
Minimum Function Test Statistic 30.918 32.074  
Degrees of freedom 24 19  
P-value (Chi-square) 0.156 0.031  
Scaling correction factor 0.964  
for the mean and variance adjusted correction (WLSMV)
```

future plans (1)

- lavaan should ‘by default’ implement best practices in all areas
 - we welcome advice from scholars
 - more simulations studies may be needed
 - ‘defaults’ settings should be flexible (depending on the model, depending on the data)
- lavaan should be 100% documented
 - every single number computed by lavaan should be documented
 - this includes the ‘mimic’ variations
 - all documentation should be available online
- lavaan should become the golden standard
 - all computations can be checked at the source code level
 - there should be a one-to-one mapping between the actual computations (at the source level) and the technical documentation

future plans (2)

- lavaan should become a computational toolbox
 - statisticians should be able to quickly (and reliably) implement their new statistical (modern) modeling ideas
 - modular, self-contained building blocks
 - application programming interface (API)
 - ...
- lavaan should be extremely fast
 - we hope to write a kernel in C++ soon
- lavaan should be available in other languages
 - python
 - Julia
 - Matlab
 - ...

future plans (3)

- lavaan should become the Rosetta stone for SEM:
 - read/parse syntax from many external programs
(we already have `mplus2lavaan()` and `lisrel2lavaan()`)
 - `lavExport()`: write/export syntax to external programs (we can already write Mplus input files)
- lavaan should be able to detect potential problems in your data and/or model automatically
 - warning and error messages should be informative
 - computing on the model (as represented by the parameter table)
- lavaan version 1.0

Thank you!

(questions?)

<http://lavaan.org>